

# Physics Prospects of Future Neutrino Oscillation Experiments

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based on works with Mayumi Aoki (Helsinki)

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and colleagues from KEK, Kyoto

## 1. Introduction to Neutrino Masses and Mixings

## 2. Present & Future of Long Baseline Neutrino Oscillation Experiments

		L/E		
K2K	KEK → SK	250 km / 1 GeV	2000 ~ 2005	
MINOS	Fermilab → Soudan	730 km / a few GeV	2005 ~	
OPERA, ICARUS	CERN → Gran Sasso	730 km / ~10 GeV	2006 ~	
JPARC → SK		300 km / 1 GeV	2009 ~	
	→ Korea	~100 km / 1 GeV	?	*
	→ <u>Hyper-Kamiokanda</u> (190 km)	300 km / 1 GeV	??	*
	→ <u>BAND@Beijing</u> (100 km)	2100 km / 4 ~ 5 GeV	???	*
	→ <u>ν Factory@JPARC</u> → <u>BAND@Beijing</u>	2100 km / 1 ~ 10 GeV	????	*

new beam line ↗

## 3. Conclusions

3 neutrino model (with Majorana masses) has

3 masses	$m_1$	$m_2$	$m_3$
3 angles	$\theta_{12}$	$\theta_{13}$	$\theta_{23}$
3 phases	$\delta_{MNS}$	$\gamma_2$	$\gamma_3$

Neutrino oscillation expt's probe

2 mass <sup>2</sup> differences	$\delta m_{12}^2 = m_2^2 - m_1^2$ , $\delta m_{13}^2 = m_3^2 - m_1^2$
3 angles	$\theta_{12}, \theta_{13}, \theta_{23}$
1 phase	$\delta_{MNS}$

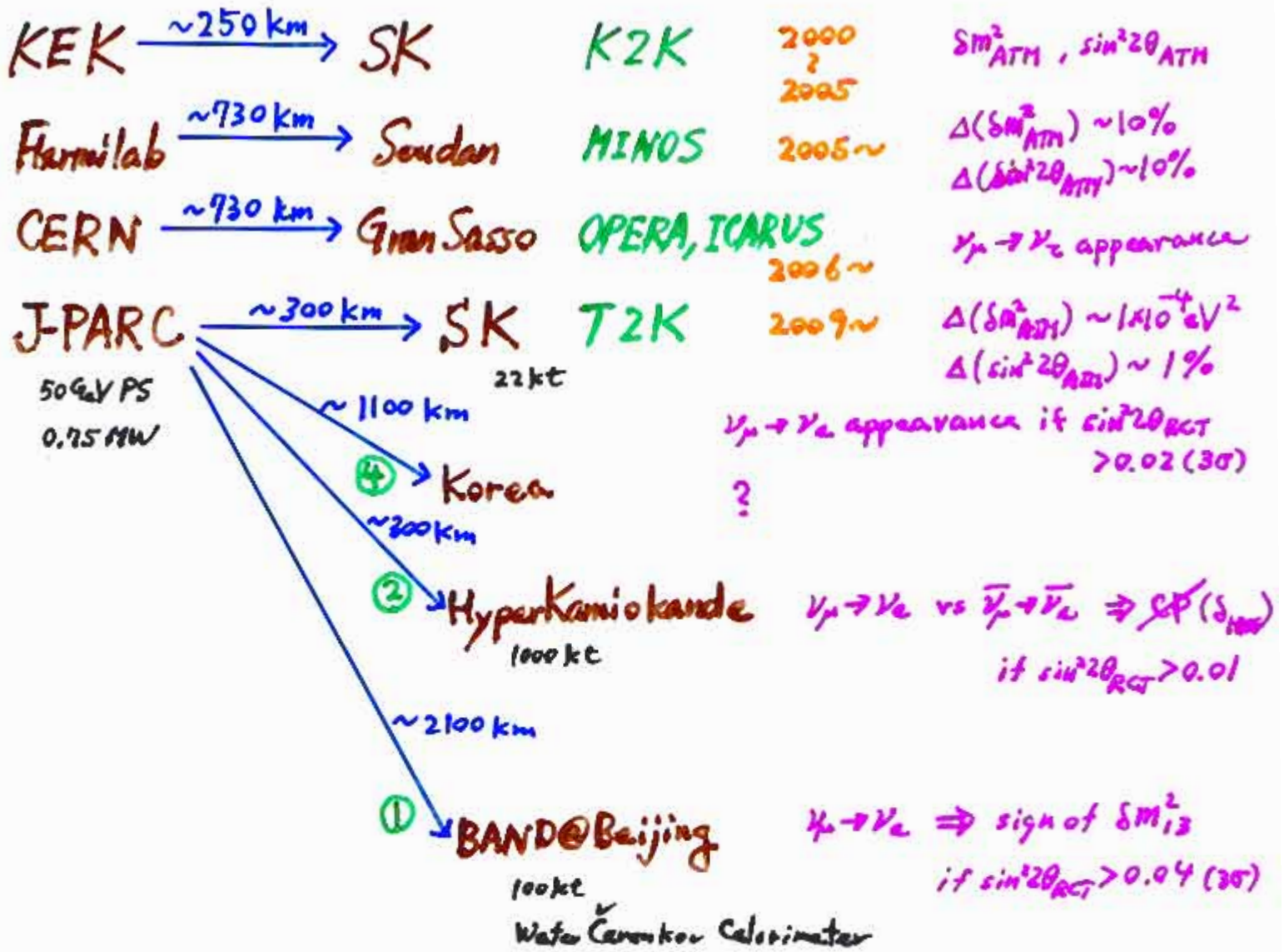
Present constraints

- $\delta m_{12}^2 = \delta m_{SOL}^2$   $(6-8) \times 10^{-5} eV^2$
- $|\delta m_{13}^2| = \delta m_{ATM}^2$   $(2-3) \times 10^{-3} eV^2$
- $4|U_{\mu 3}|^2(1-|U_{\mu 3}|^2) = \sin^2 2\theta_{ATM}$   $0.9-1$
- $4|U_{e 2}|^2(1-|U_{e 2}|^2) = \sin^2 2\theta_{SOL}$   $0.7-0.9$
- $4|U_{e 3}|^2(1-|U_{e 3}|^2) = \sin^2 2\theta_{RCT}$   $< 0.1$
- $\delta_{MNS}$   $\text{no constraint}$

Targets of future neutrino oscillation experiments

- measure  $\sin^2 \theta_{RCT}$
- measure  $\delta_{MNS}$
- determine the sign of  $\delta m_{13}^2$   $(m_3^2 \gtrless m_1^2)$
- determine the sign of  $\sin^2 \theta_{ATM} - \frac{1}{2}$   $(\sin^2 \theta_{ATM} \gtrless 0.5)$
- more precise measurements  $|U_{\mu 3}|^2$

# Present and future LBL neutrino oscillation experiments



- ① M. Aoki et al., hep-ph/0112328 ; PRD69:093004 (2003)
- ② M. Aoki, KH, N. Okamura, hep-ph/0208227 ; PLB554:121-122 (2003)
- ③ M. Aoki, KH, N. Okamura, hep-ph/0311324
- ④ KH, K. Senda, N. Okamura



K 2 K

2000 ~ 2005

$$\frac{L}{E} \approx \frac{250 \text{ km}}{1 \text{ GeV}} \approx 250 \text{ (km/GeV)}$$

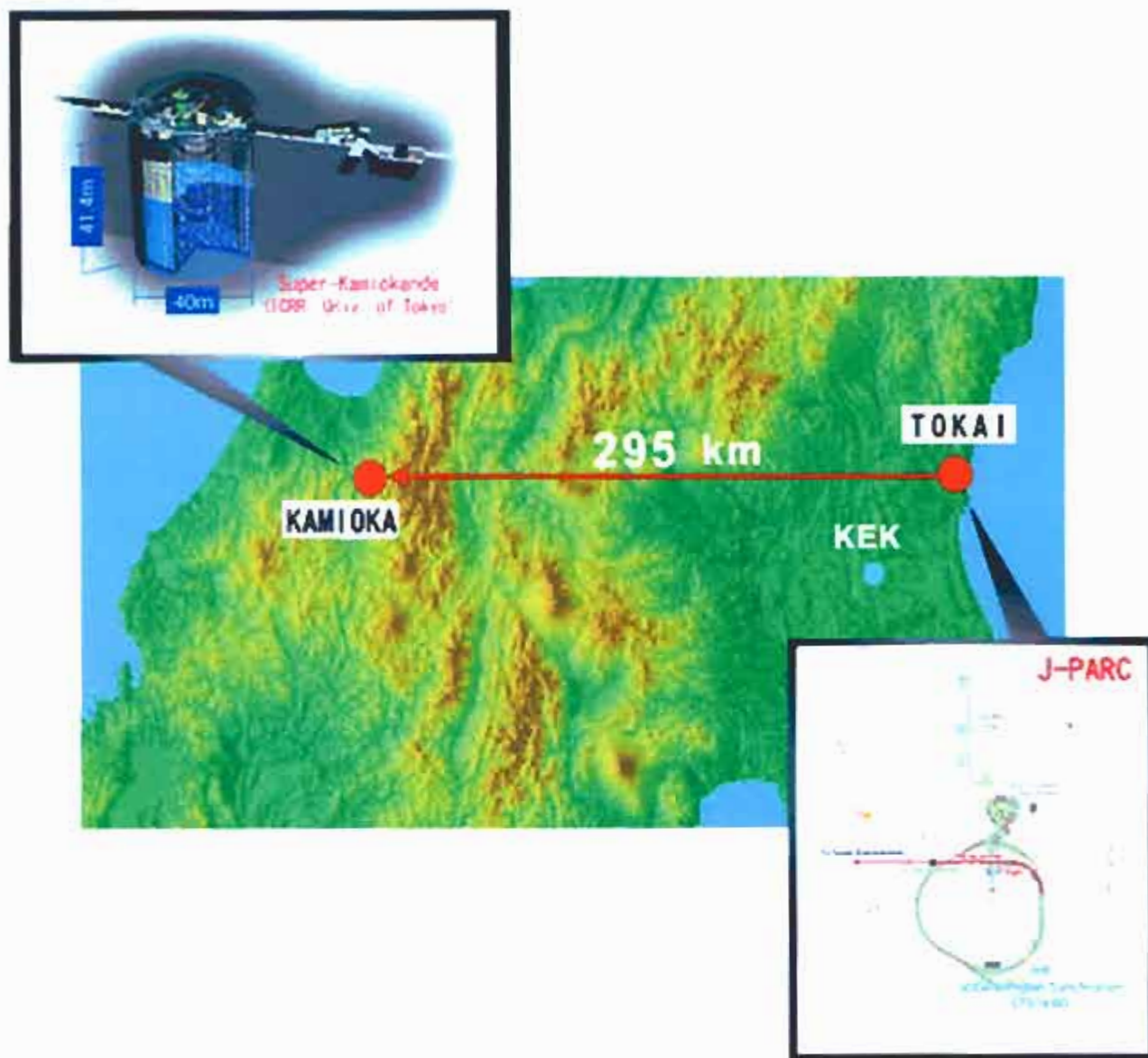
$10^{20}$  POT in 5 years

$$\Rightarrow P(\nu_\mu \rightarrow \nu_\mu) = 1 - \sin^2 2\theta_{ATM} \sin^2 \left( \frac{\delta m_{ATM}^2}{4E} L \right)$$

$$0.6 \times \frac{\pi}{2} \dots \delta m^2 = 3 \times 10^{-3} \text{ eV}^2$$

$$0.5 \times \frac{\pi}{2} \dots \delta m^2 = 2.5 \times 10^{-3} \text{ eV}^2$$

$$0.4 \times \frac{\pi}{2} \dots \delta m^2 = 2 \times 10^{-3} \text{ eV}^2$$



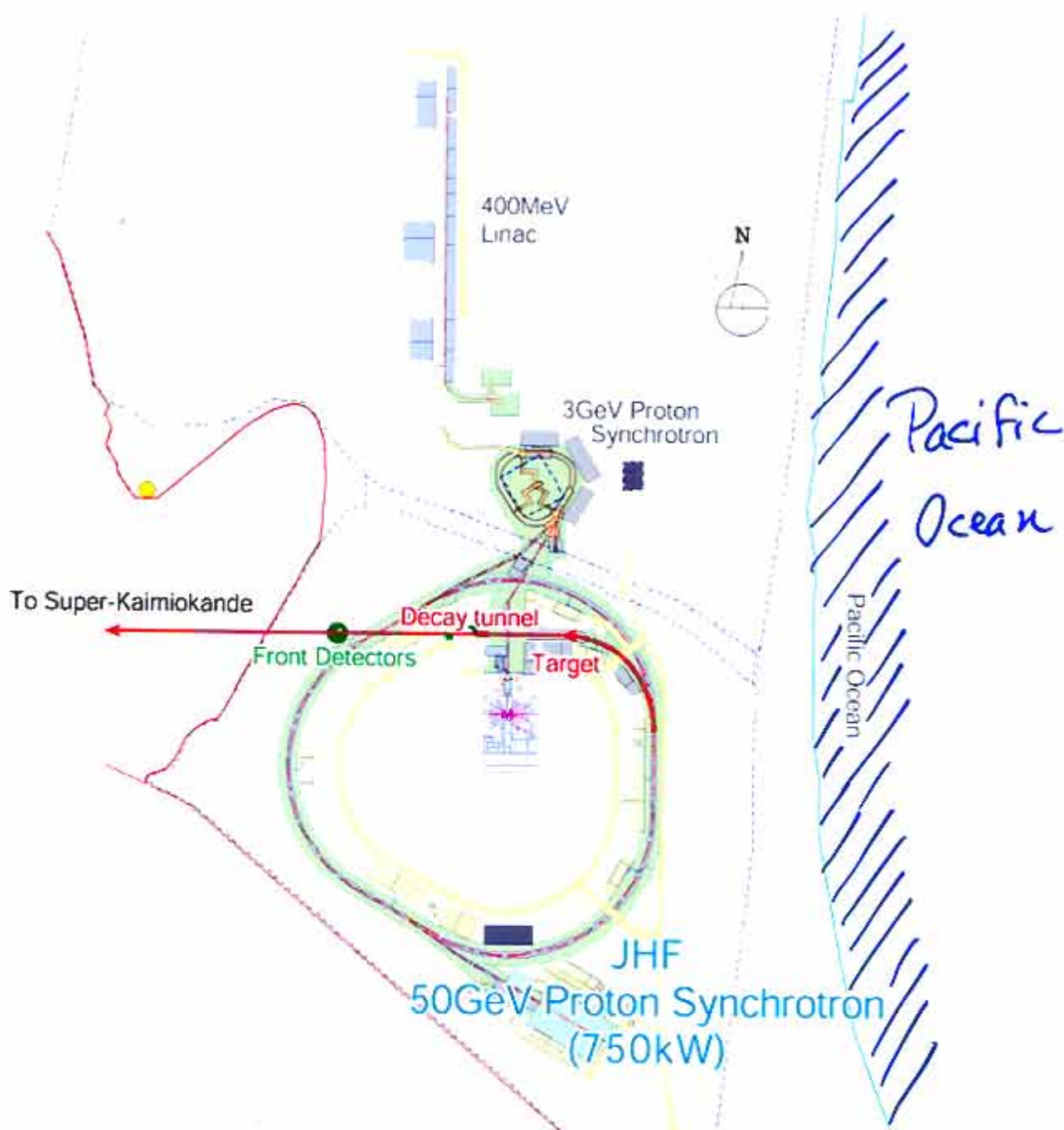
# JPARC-to-SK 2009~

$$\frac{L}{E} \approx \frac{300 \text{ km}}{1 \text{ GeV}} \approx 300 \text{ (km/GeV)}$$

$10^{21}$  POT in 1 year 50 times K2K!

- Precise measurement of  $\delta m^2_{\text{ATM}}$ ,  $\sin^2 2\theta_{\text{ATM}}$
- Discovery of  $\nu_{\mu} \rightarrow \nu_e$  oscillation  $\sin^2 2\theta_{\text{RCT}} \gtrsim 0.02$  (3 $\sigma$ )

cf. <http://neutrino.kek.jp/jhfnu/>



# JPARC

Japan Proton Accelerator Research Complex

[close](#)

# Off Axis Beam

(ref.: BNL-E889 Proposal)

- ◆ Quasi Monochromatic Beam
- ◆ x 2~3 intense than NBB

**Tuned at oscillation maximum**

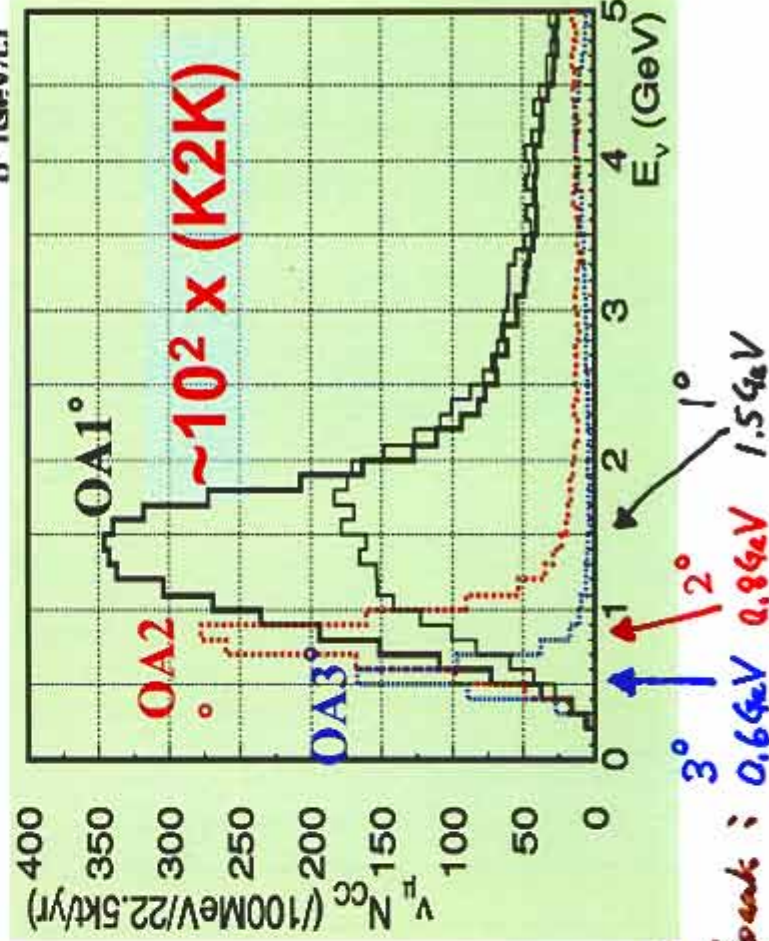
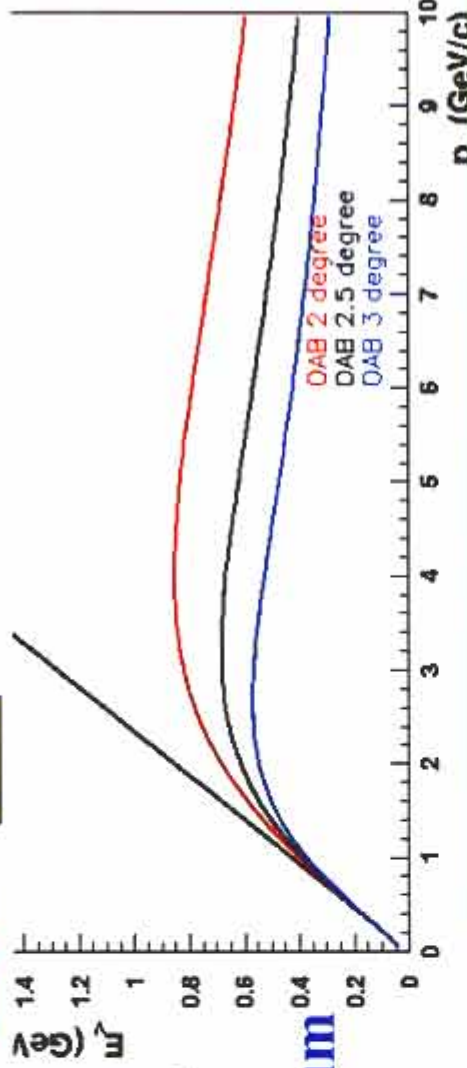
## Statistics at SK

(OAB 2 deg, 1 yr, 22.5 kt)

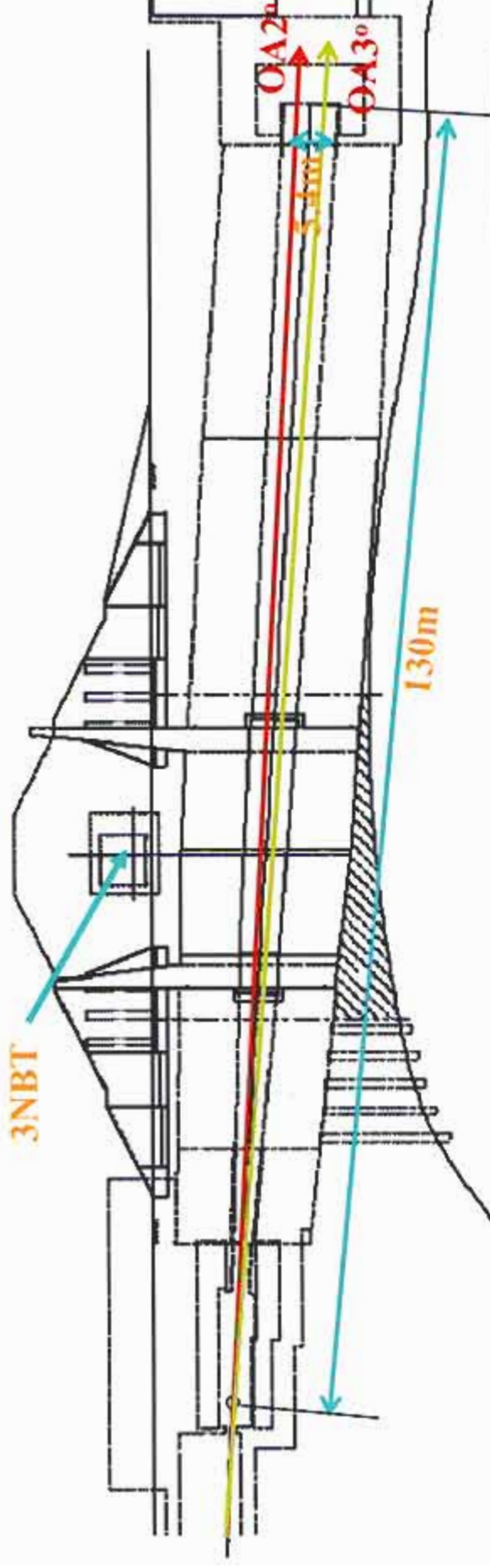
~ 4500  $\nu_\mu$  tot

~ 3000  $\nu_\mu$  CC

$\nu_e$  ~0.2% at  $\nu_\mu$  peak



# Decay volume



- Cover OAB 2~3deg.
  - Peak Ev ~ 500-800MeV
- Helium filled to reduce absorption.
- Water-cooled He vessel inside concrete shield
- Start construction of crossing part: May 2004

He vessel wall equipped w/ water piping





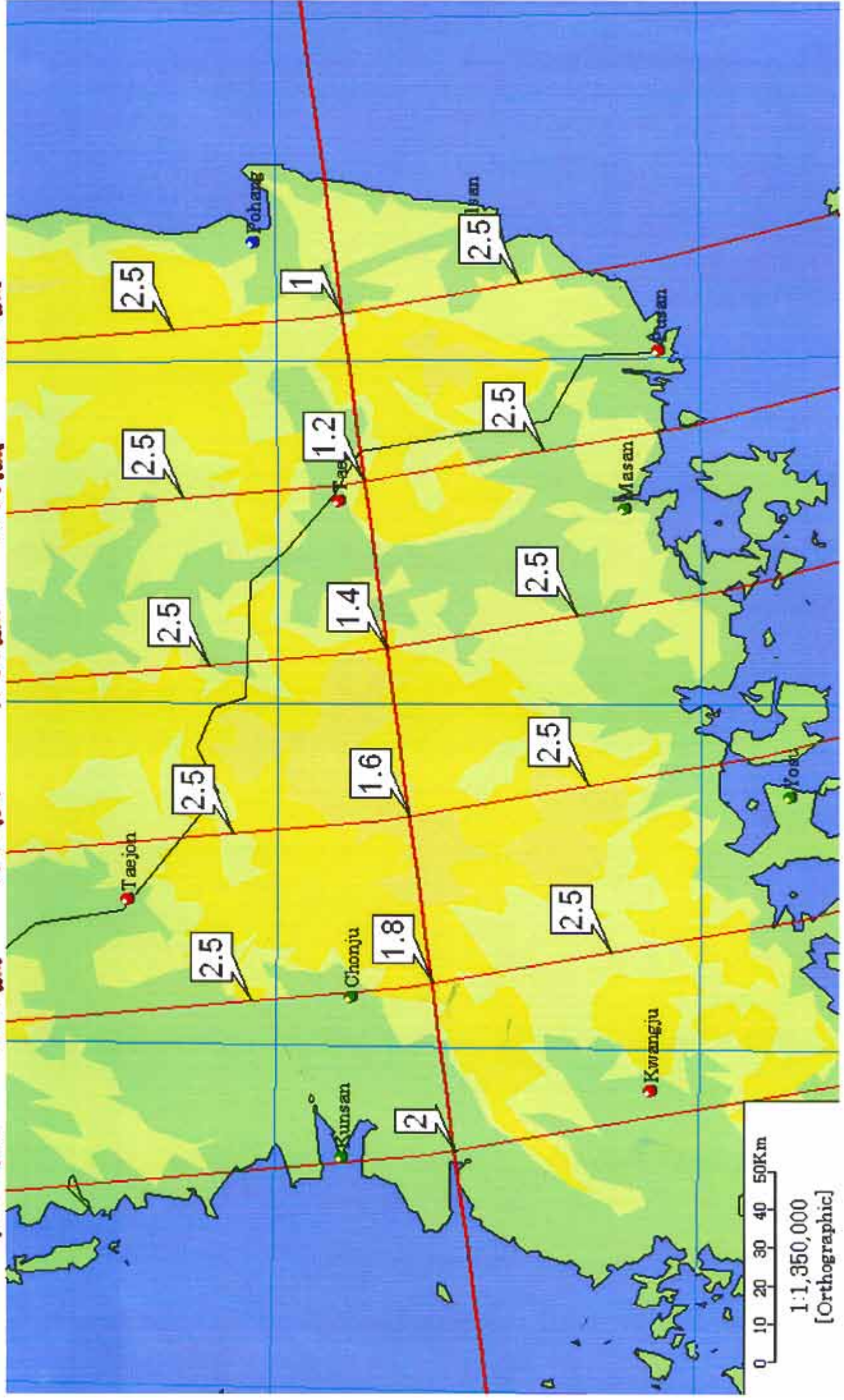
# Fate of OA 2.5° beam from J-PARC



$L = 295 \text{ km}$   
 SK (+329m above the sea level)

by Keiichi Senda

$L =$   
 1256 km    1211 km    1166 km    1122 km    1077 km    1032 km    1000 km



1:1,350,000  
 [Orthographic]

KOREA

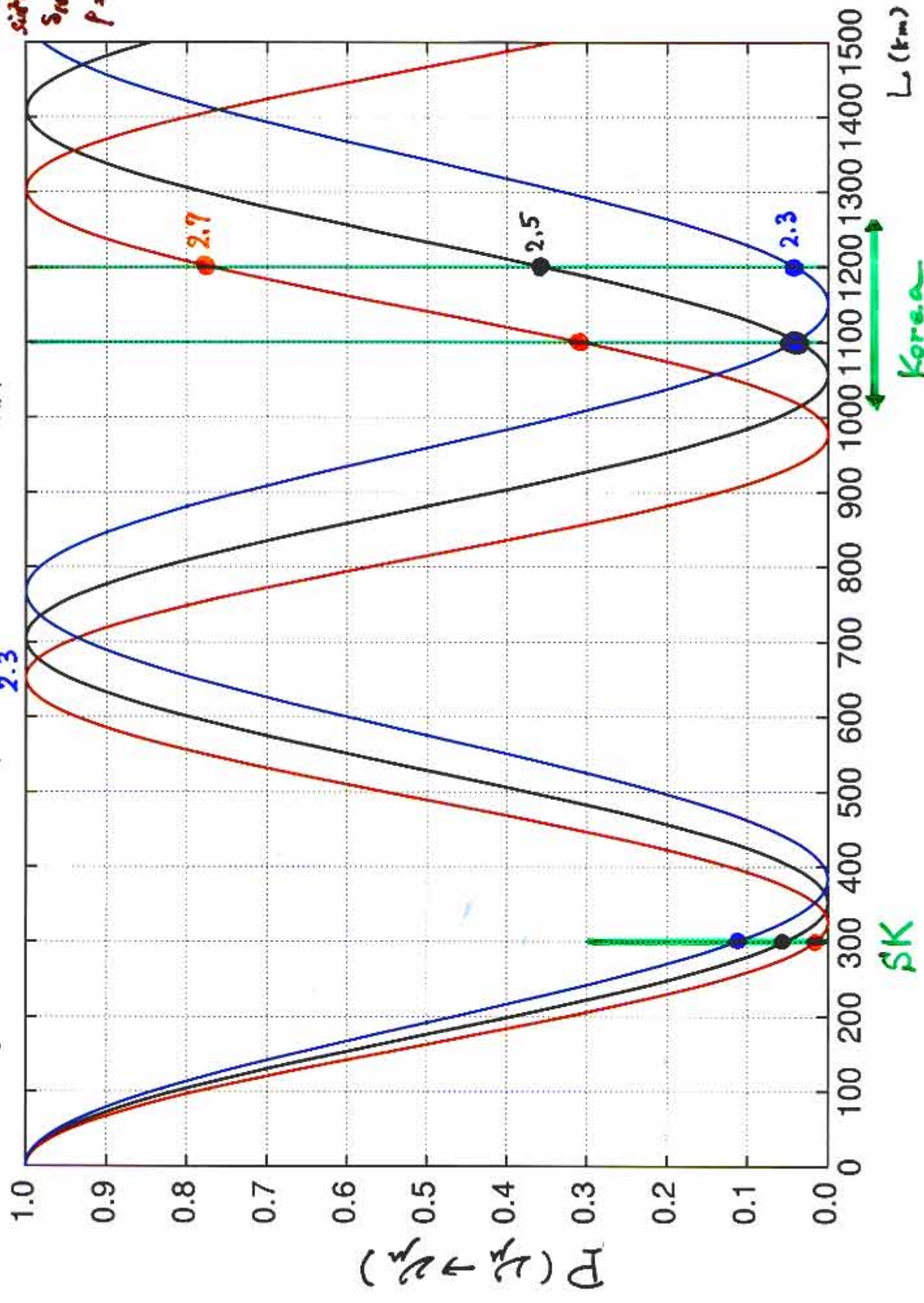
by Kavericki Souda

$\sin^2 \theta_{sol} = 7.0 \times 10^{-6}$   
 $\sin^2 2\theta_{sol} = 0.8$   
 $\delta_{MNS} = 0^\circ$   
 $\rho = 3.9 / \text{cm}^3$

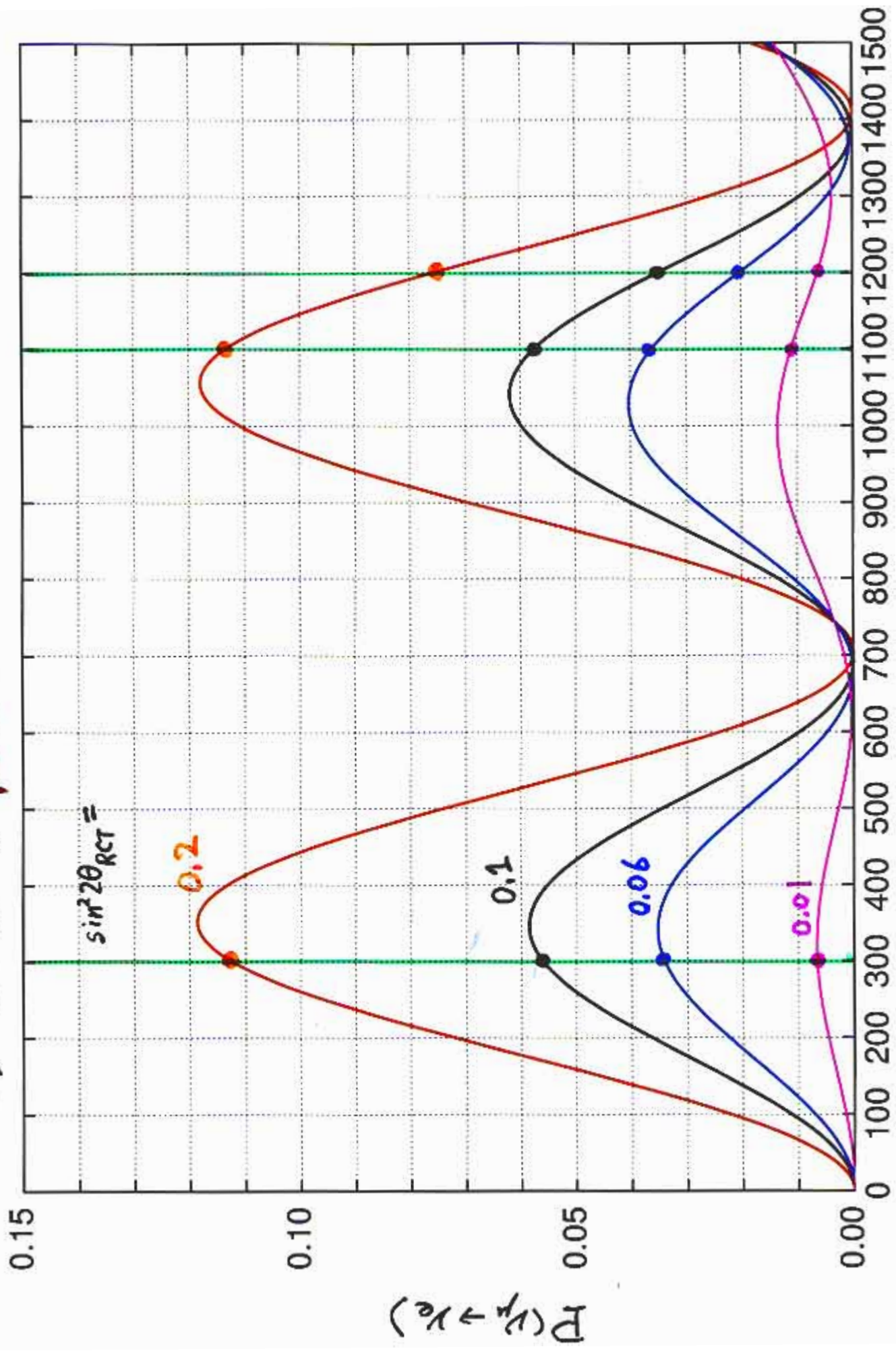
$\sin^2 2\theta_{ATM} = 1$

$\delta m_{ATM}^2 = 2.5 \times 10^{-3} \text{ eV}^2$   
 2.7  
 2.3

$E_\nu = 0.7 \text{ GeV}$



$E_\nu = 0.7 \text{ GeV}$  ( $\sim E_{\text{peak}}$  of OA  $2.5^\circ$ )



# Measuring $\delta_{MNS}$ by LBL experiments

J-PARC  $\rightarrow$  Hyper-Kamiokande

M. Aoki, K.H., N. Okamura

hep-ph/0208223

PLB554, 121 (2003)

\* Update: NBB  $\rightarrow$  OAB

J-PARC  $\simeq$   $10^{21}$  POT/year  $\simeq 50 \times$  K2K

HK 1000 kt water Čerenkov  $\simeq 50 \times$  SK

case study

$\nu_{\mu}$  OAB  $2^\circ$  1 year

$\bar{\nu}_{\mu}$  OAB  $2^\circ$  4 years

$\nu_{\mu}$  OAB  $3^\circ$  1 year  $\leftarrow$  necessary to resolve  $\delta = 0^\circ$  from  $180^\circ$

BG from secondary beam contributions  
20% mis-identification (neutral currents)

eff  $\simeq 2\%$   $sp = 3.3\%$

We find

$$\delta_{MNS}^{true} = 90^\circ, 270^\circ$$

$\downarrow$

$$\Delta\delta_{MNS} = \pm 30^\circ$$

CP can be established at 4 $\sigma$

if  $|s|, |s-180^\circ| > 30^\circ$

$$\sin^2 2\theta_{RCT} > 0.02$$

$$\delta_{MNS}^{true} = 0^\circ, 180^\circ$$

$\downarrow$

$$\Delta\delta_{MNS} = \pm 9^\circ$$

$0^\circ$  vs  $180^\circ$  degeneracy

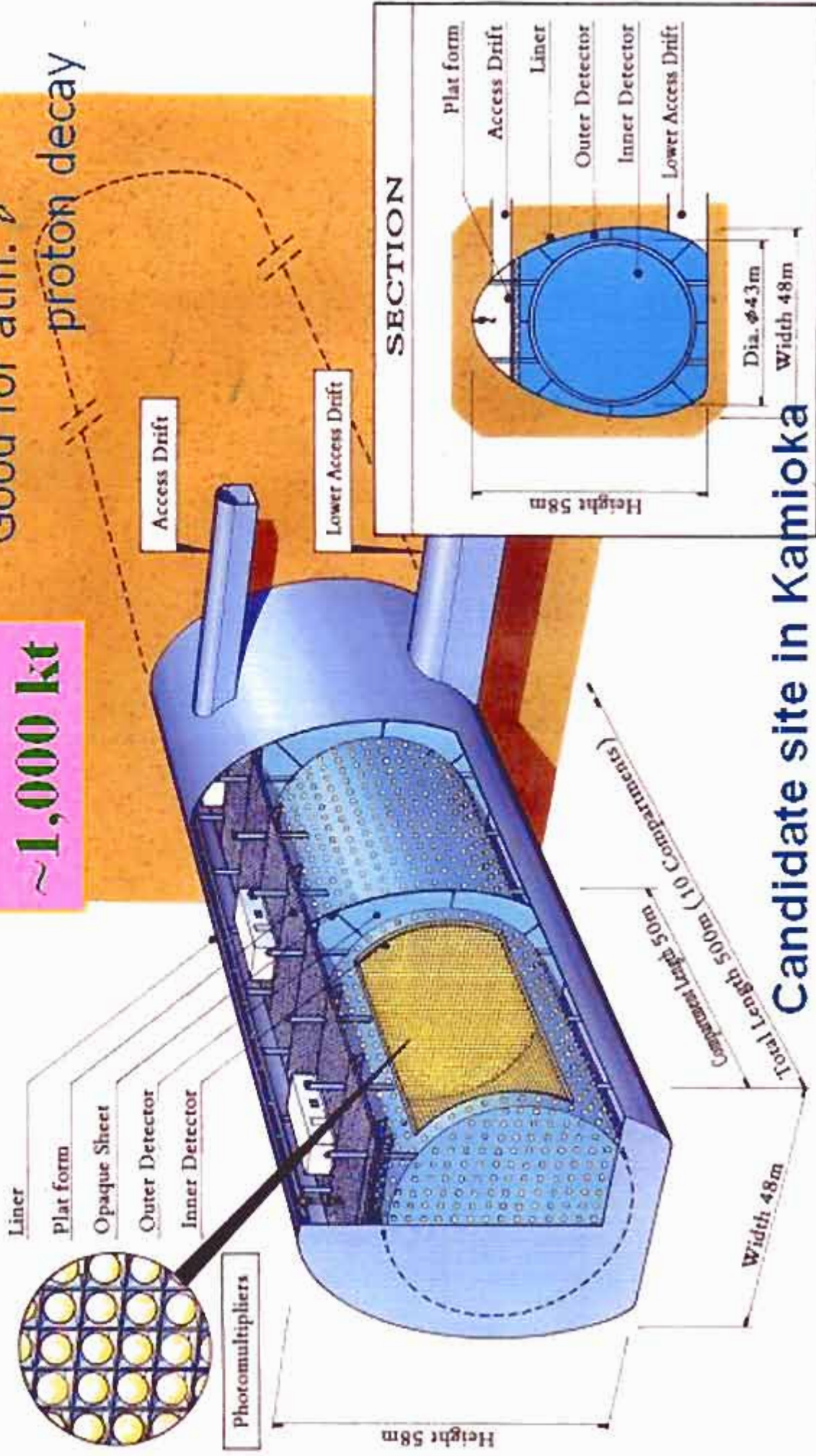
$$OAB2 + OAB3 \Rightarrow 25 (\sin^2 2\theta_{RCT} \sim 0.06)$$

$$15 ( \quad \sim 0.01)$$

# Hyper-Kamiokande (a far detector in the 2nd phase)

Good for atm.  $\nu$   
proton decay

~1,000 kt

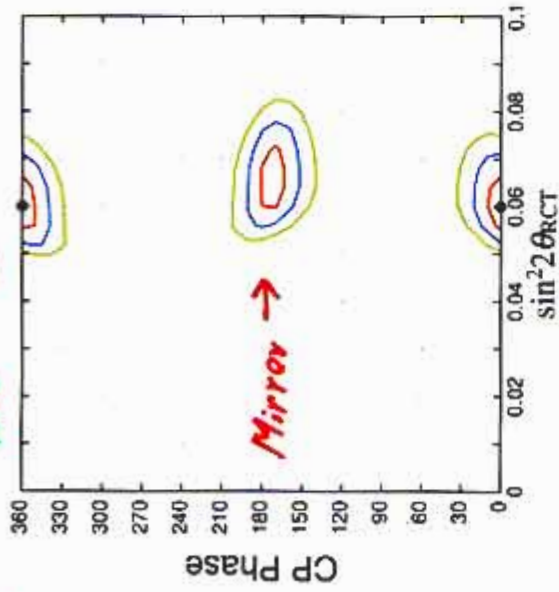


Candidate site in Kamioka

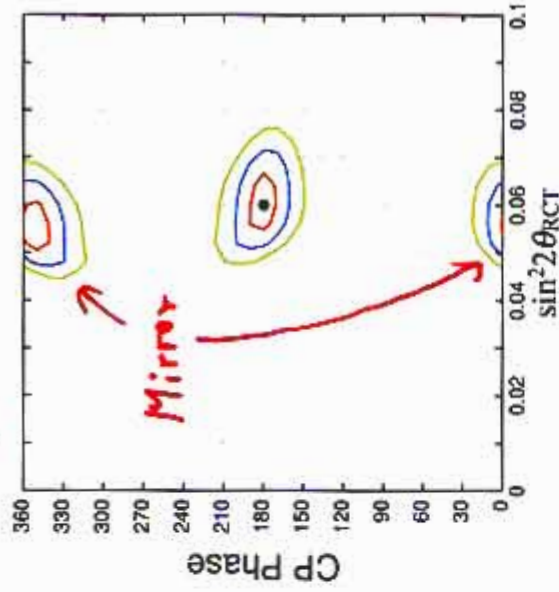
Ambiguity between

$\delta = 0^\circ \leftrightarrow 180^\circ$

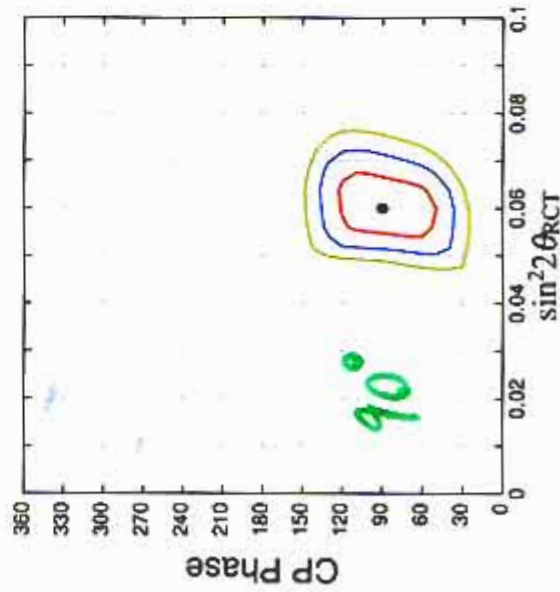
True  $\delta_{MNS} = 0^\circ$



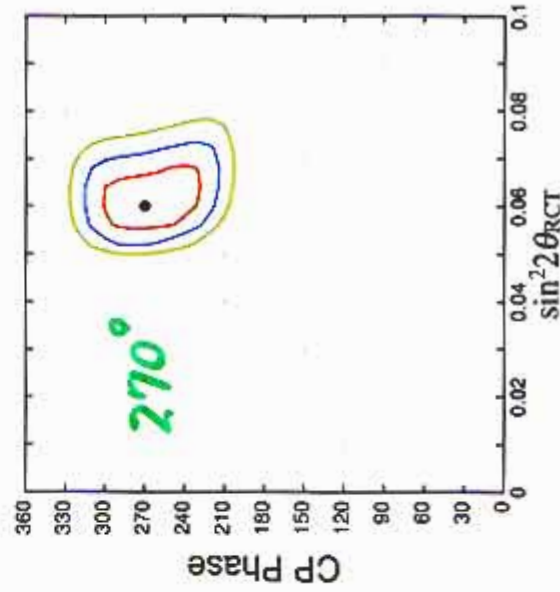
$180^\circ$



$\chi^2_{\mu}$  (OAZ $^\circ$ )  
 (year)  
 +  
 $\chi^2_{\nu}$  (OAZ $^\circ$ )  
 (4 years)



$90^\circ$

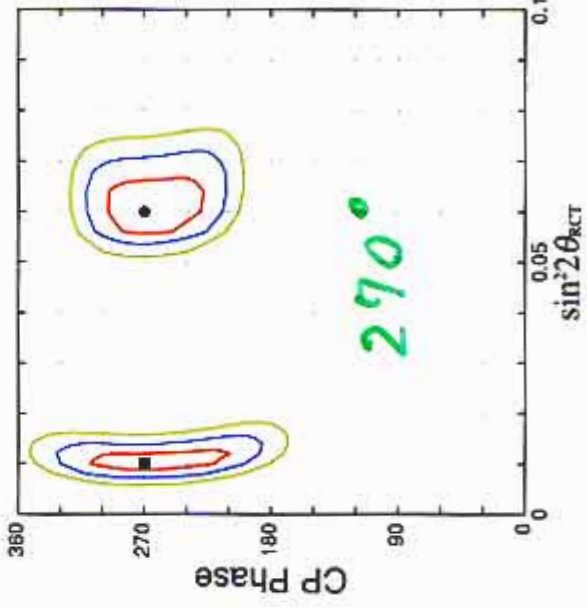
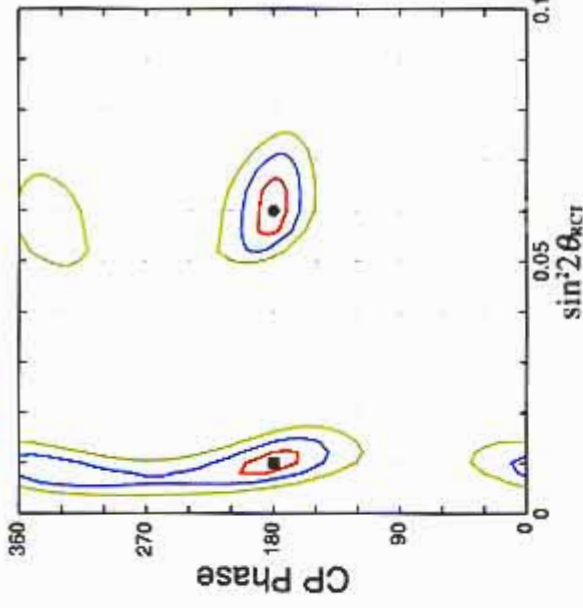


$270^\circ$

$\sin^2 2\theta_{RCT}^{true} = 0.06$

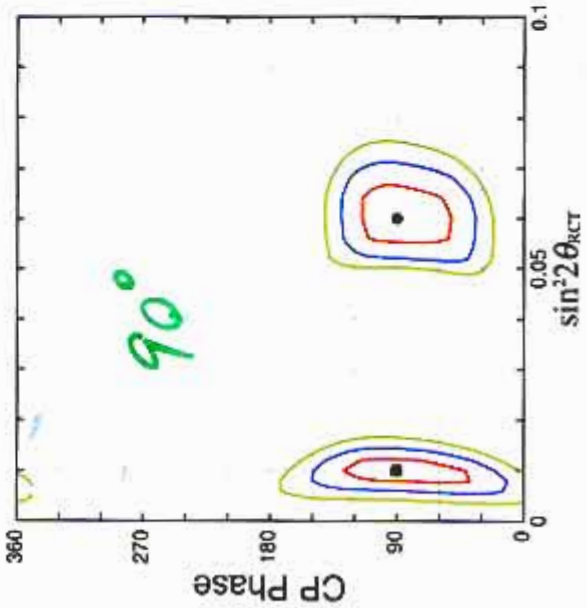
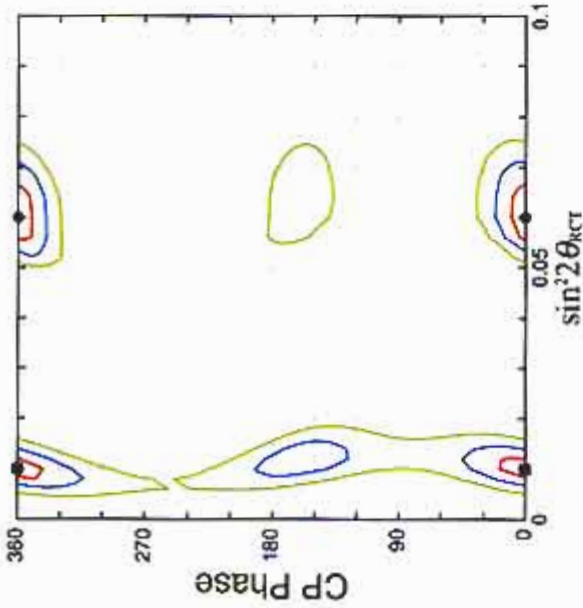
$$\chi^2_{\mu}(\text{OAZ}^{\circ})_{1\text{ year}} + \chi^2_{\mu}(\text{OAZ}^{\circ})_{4\text{ years}} + \chi^2_{\mu}(\text{OAZ}^{\circ})_{1\text{ year}}$$

180°



270°

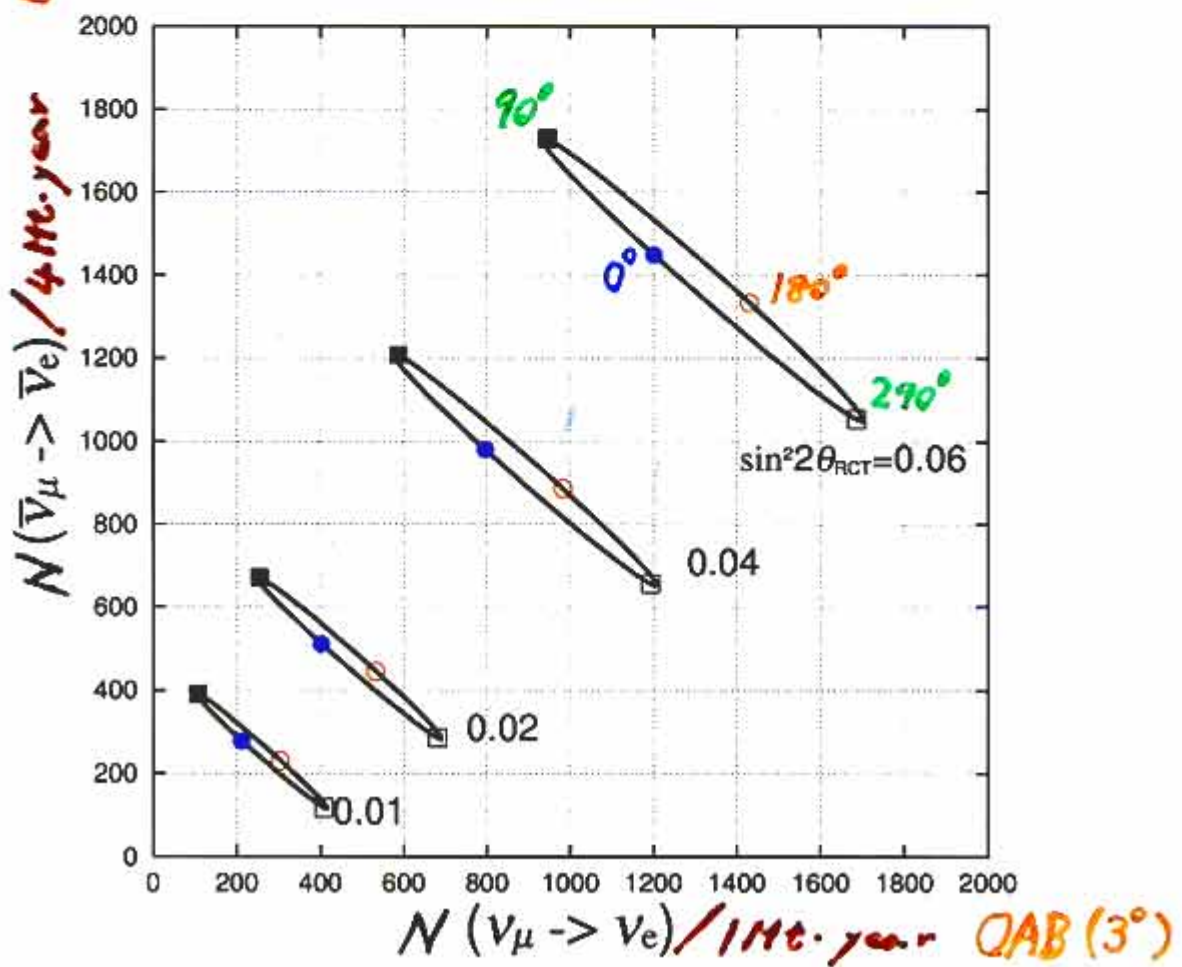
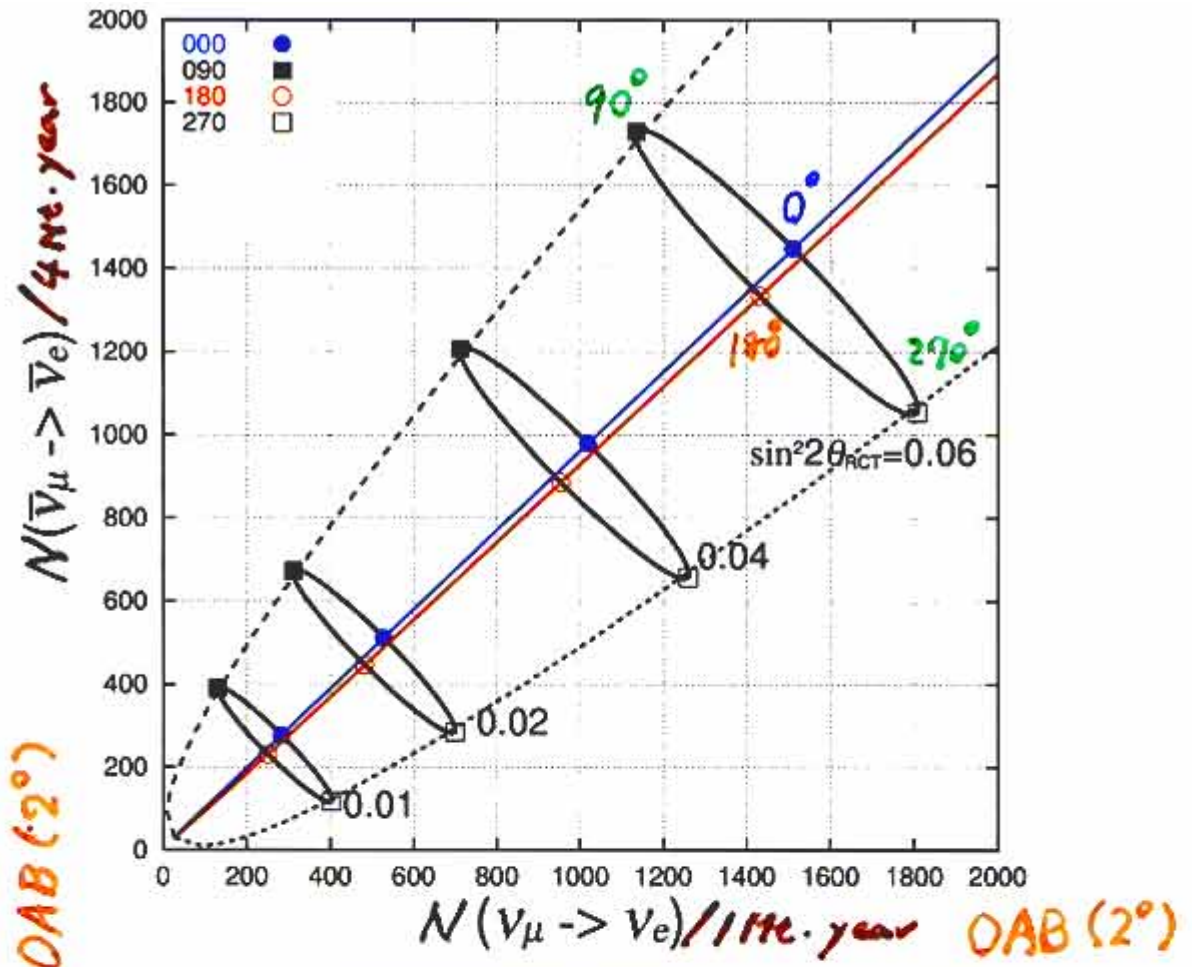
$S_{\text{MNS}}^{\text{trans}} = 0^{\circ}$



90°

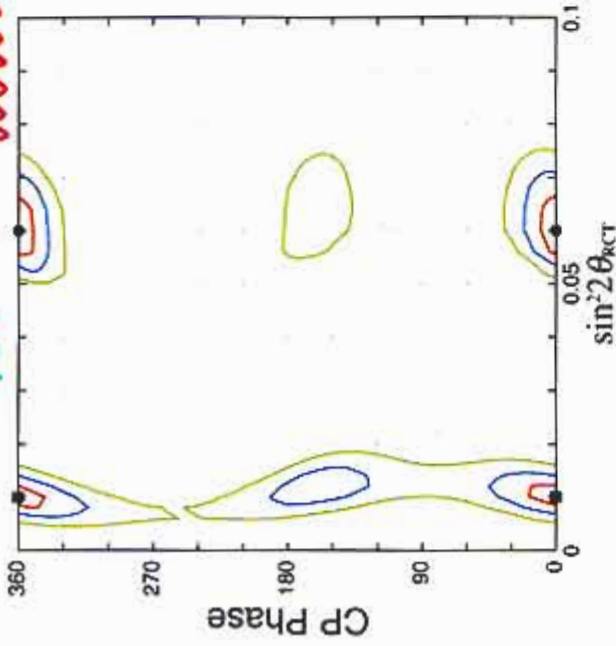
$$\sin^2 2\theta_{\text{RCT}}^{\text{trans}} = 0.01, 0.06$$





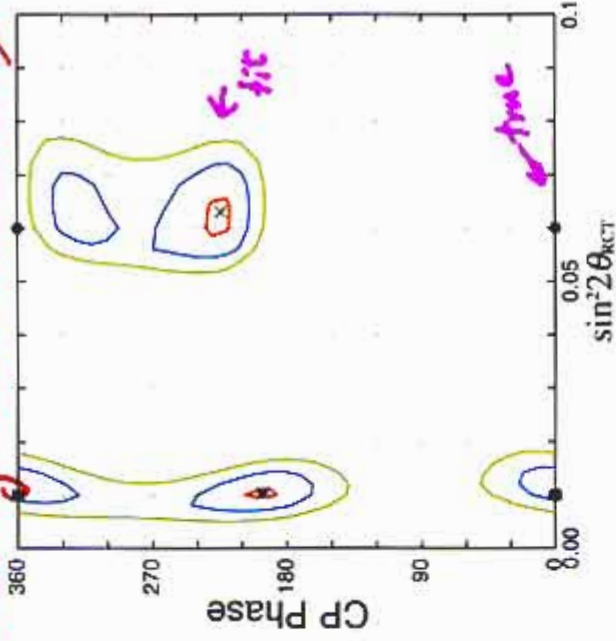
**HOWEVER**

$\delta_{MNS}^{true} = 0^\circ$   $\delta_{MNS}^{true} > 0$

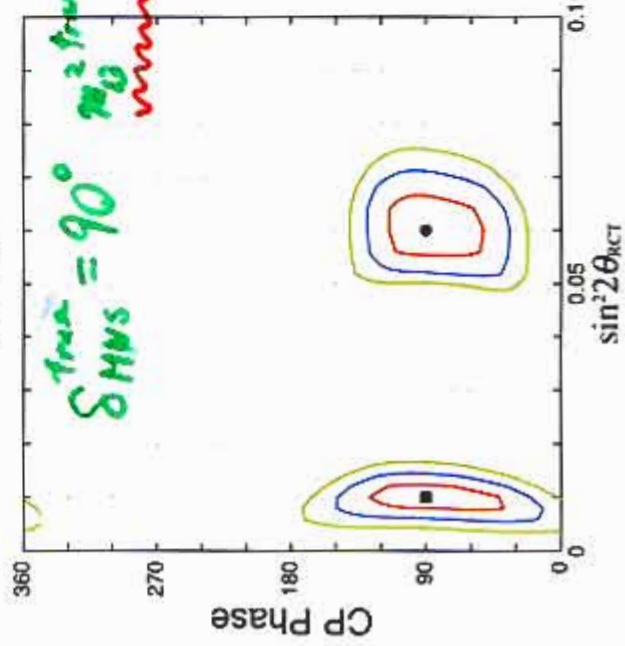


If the same data is analyzed by assuming the inverted hierarchy:  $\delta_{MNS}^{true} < 0$

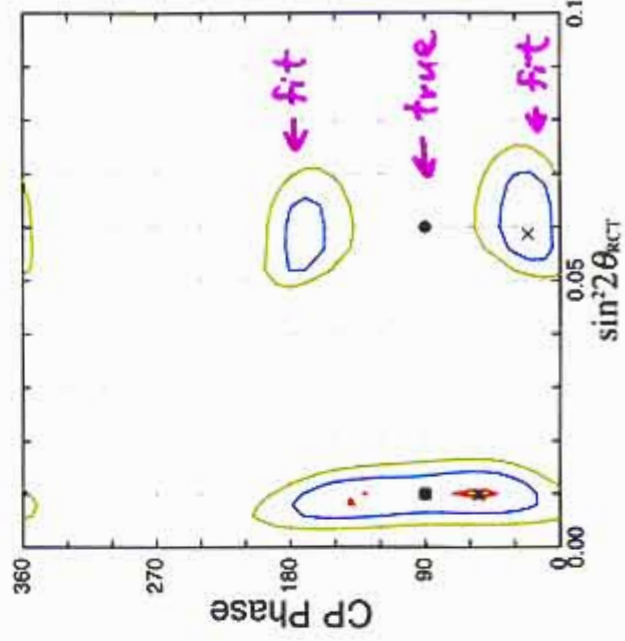
CP?



$\delta_{MNS}^{true} = 90^\circ$   $\delta_{MNS}^{true} > 0$



No CP?

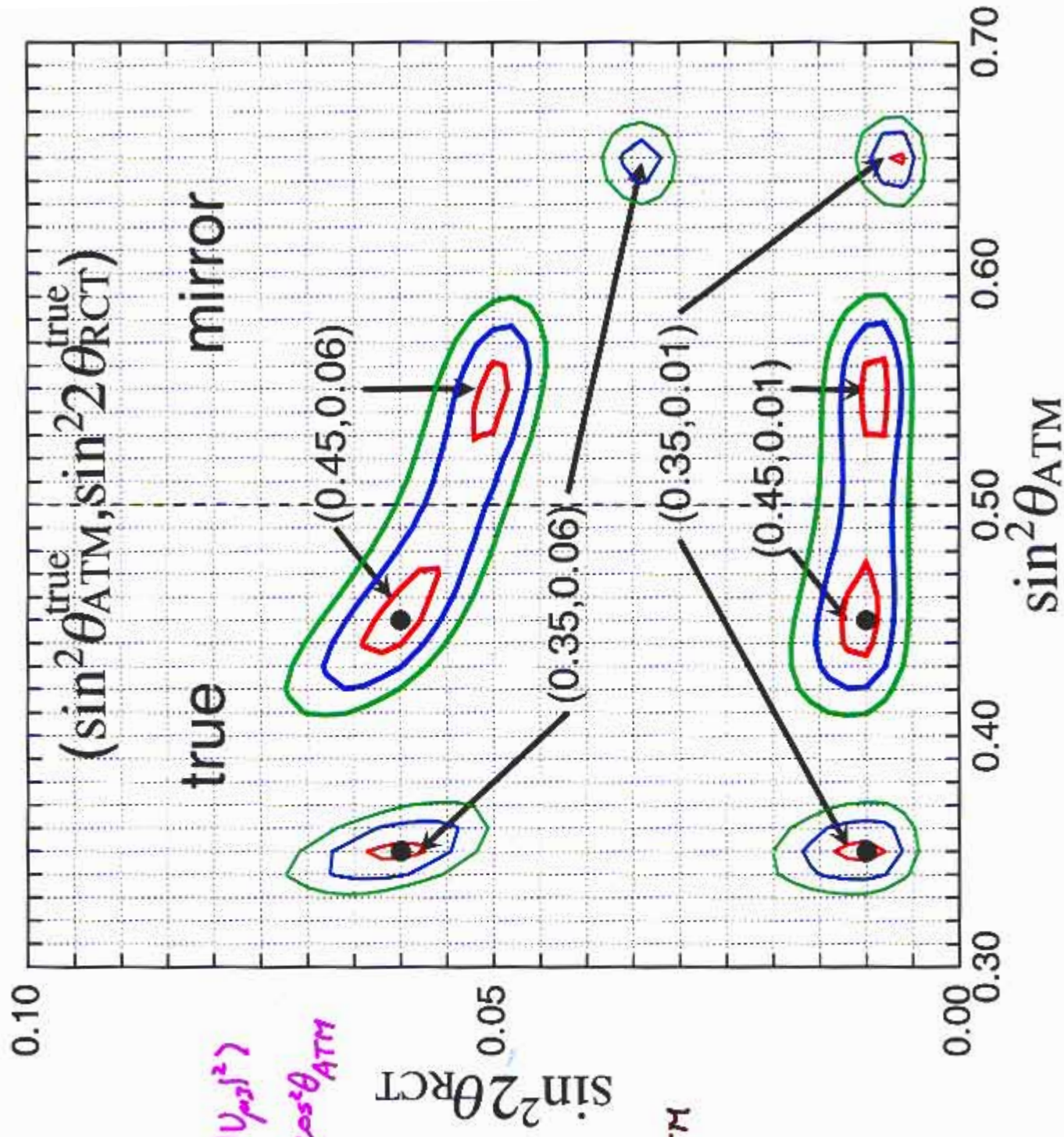


$\sin^2 2\theta_{KCT}^{true} = 0.01, 0.06$

More ambiguity ③  $\sin^2 \theta_{ATM} \lesssim 0.5$

$$\begin{aligned} \sin^2 2\theta_{ATM} &= 4 |V_{\mu 3}|^2 (1 - |V_{\mu 2}|^2) \\ &= 4 \sin^2 \theta_{ATM} \cos^2 \theta_{ATM} \end{aligned}$$

$\sin^2 \theta_{ATM}$	$\sin^2 2\theta_{ATM}$
0.35	→ 0.91
0.40	→ 0.96
0.45	→ 0.99



In order to resolve the mass hierarchy ambiguity

$$m_1^2 < m_3^2 \quad \text{normal } (\delta m_{13}^2 > 0)$$

$$m_1^2 > m_3^2 \quad \text{inverted } (\delta m_{13}^2 < 0)$$

we need to make use of the earth matter effect

↓  
higher  $E$  ✓  
↓  
longer  $L$

**BAND @ Beijing** has been proposed: Y. Li Wang, hep-ex/0010051  
 100 kt Water Čerenkov Calorimeter Y. Li Wang et al, PRD65: 093021 (2002)

$$L = 2,100 \text{ km}$$

We examined the possibility of using High-Energy, Narrow Band-Beam  
 from **J-PARC**  $\langle E_\nu \rangle \sim 3 - 5 \text{ GeV}$  new beam line

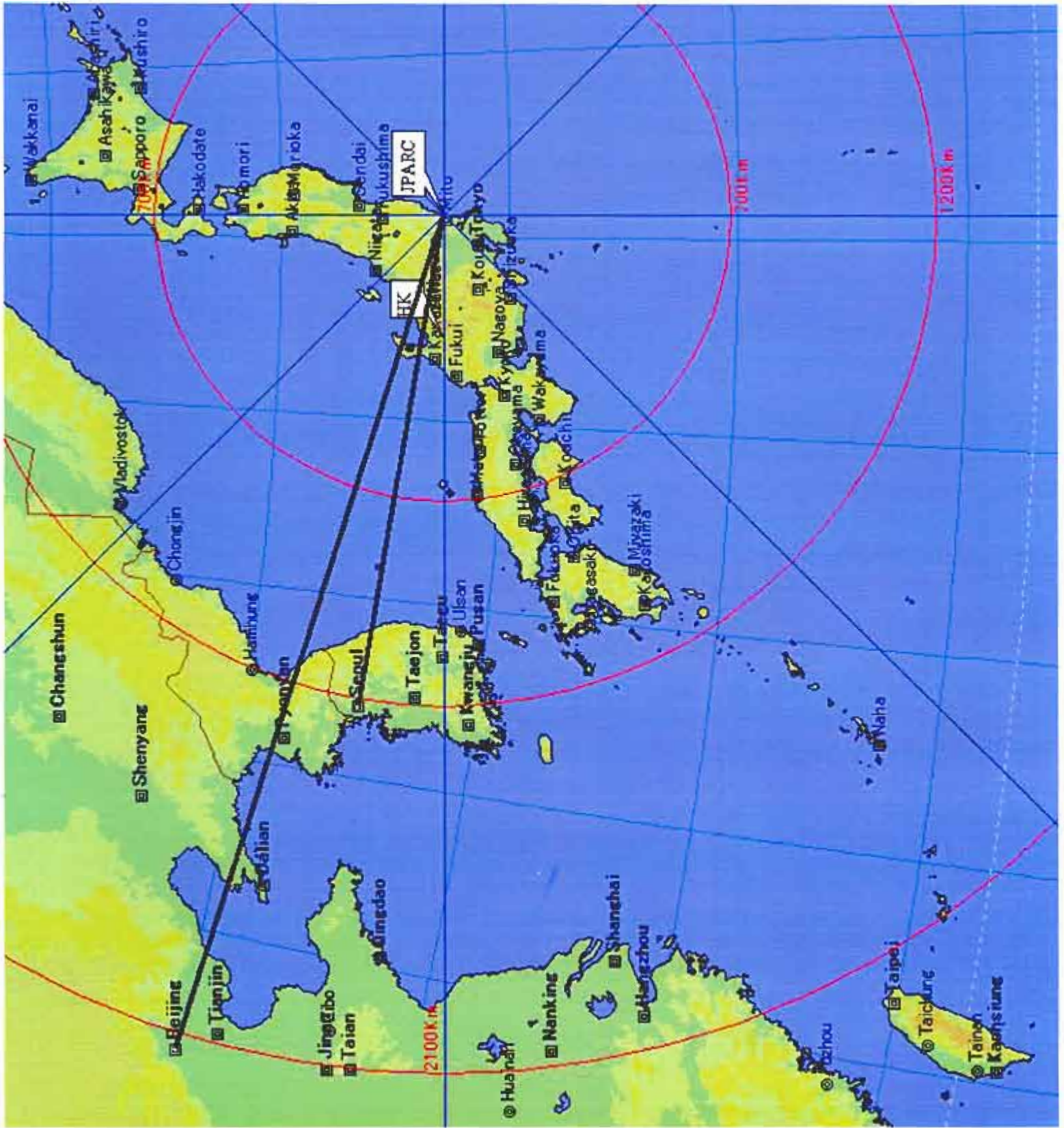
We find

$$P(\nu_\mu \rightarrow \nu_e)_{\delta m_{13}^2 < 0} \ll P(\nu_\mu \rightarrow \nu_e)_{\delta m_{13}^2 > 0}$$

If  $\nu_\mu \rightarrow \nu_e$  is observed Both at SK and at BAND,  
 then  $\delta m_{13}^2 > 0$  can be established.

$$m_3^2 > m_1^2 \text{ resolved if } \sin^2 2\theta_{\text{RCT}} > 0.04 (3\sigma)$$

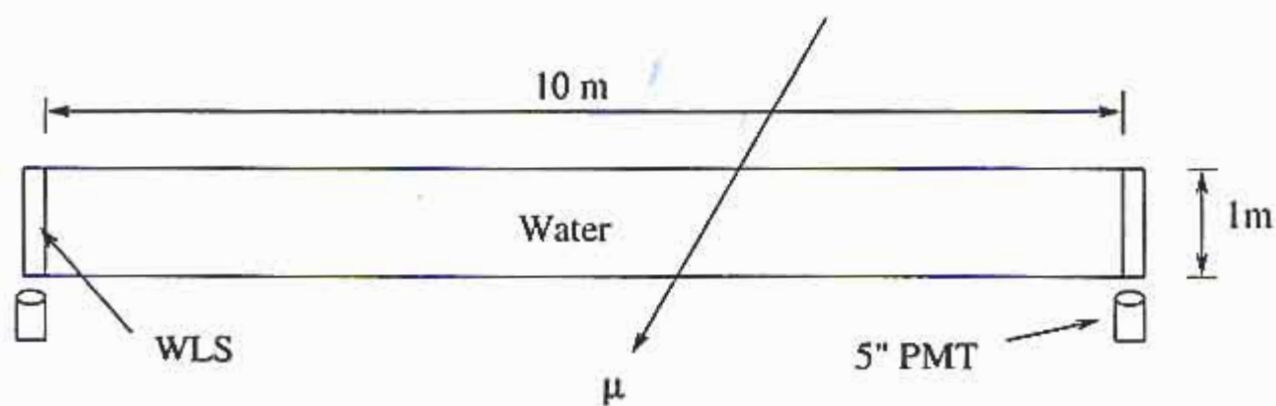
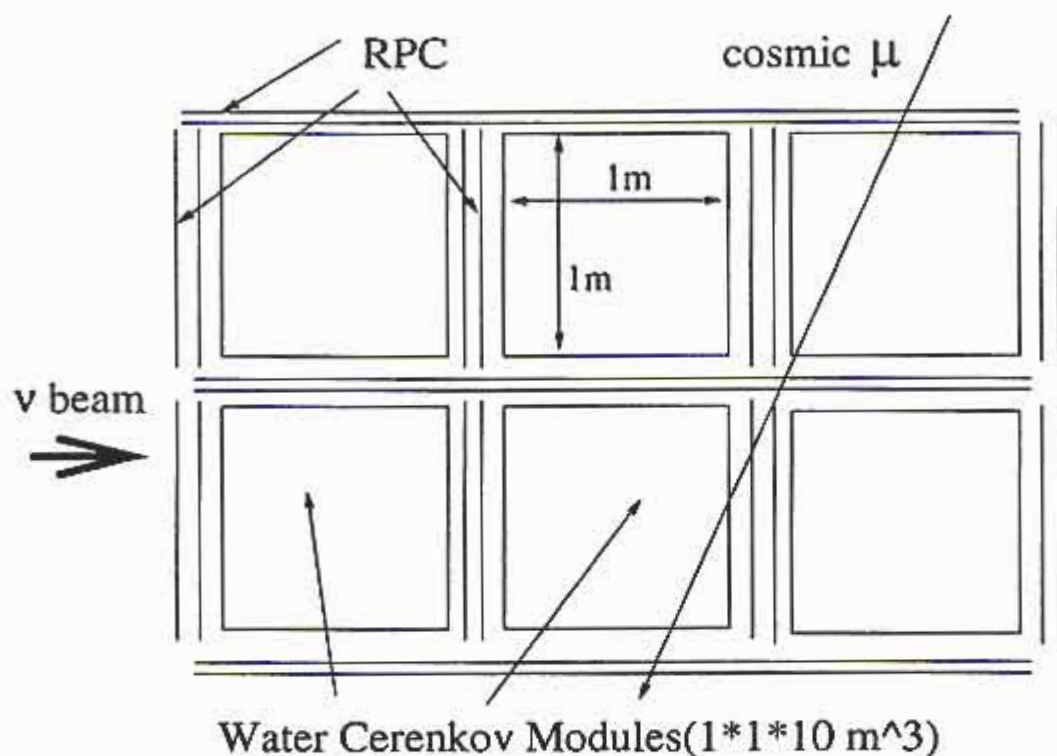
Y. Akai-KH-Hayato Kobayashi-Nishikawa-Ogawa et al,  
 PRD69: 092004 (2003)



# Beijing Astrophysics & Neutrino Detector

Y. F. Wang, hep-ex/0010081

Y. F. Wang, K. Whisnant, B. L. Young,  
PRD65:073021(2002)

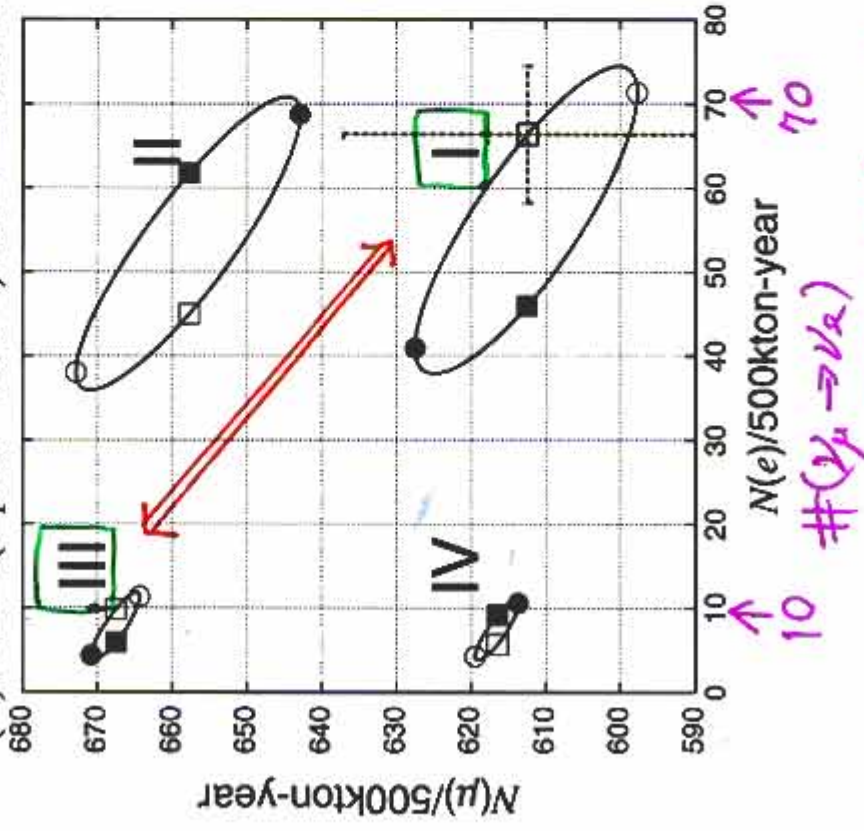


(1m x 1m x 10m) unit

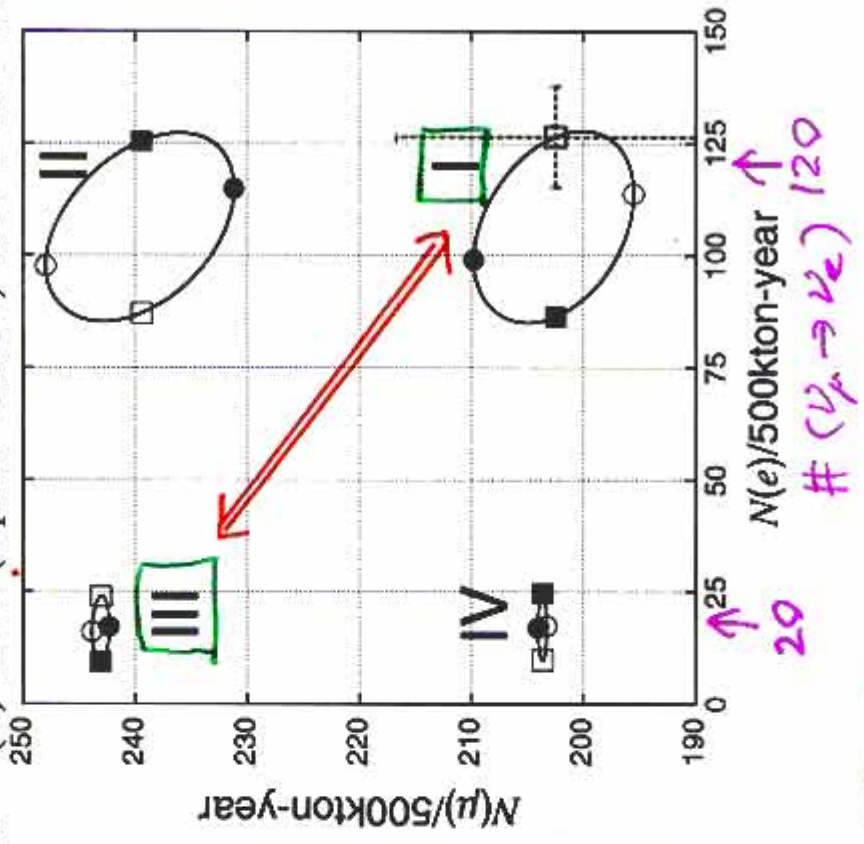
2100 km

Inputs :  $\delta m_{ATM}^2 = 3.5 \times 10^{-3} \text{ eV}^2$      $\sin^2 2\theta_{ATM} = 1$   
 $\delta m_{SOL}^2 = 1 \times 10^{-4} \text{ eV}^2$      $\sin^2 2\theta_{SOL} = 0.8$   
 $\delta m_{MS} = 0^\circ - 90^\circ - 180^\circ - 270^\circ - 360^\circ$      $\sin^2 2\theta_{CHOZ} = 0.1$   
 $\rho = 3\delta / \text{cm}^3$

(a) NBB ( $E_{\text{peak}}=4\text{GeV}$ ) at  $L=2100 \text{ km}$



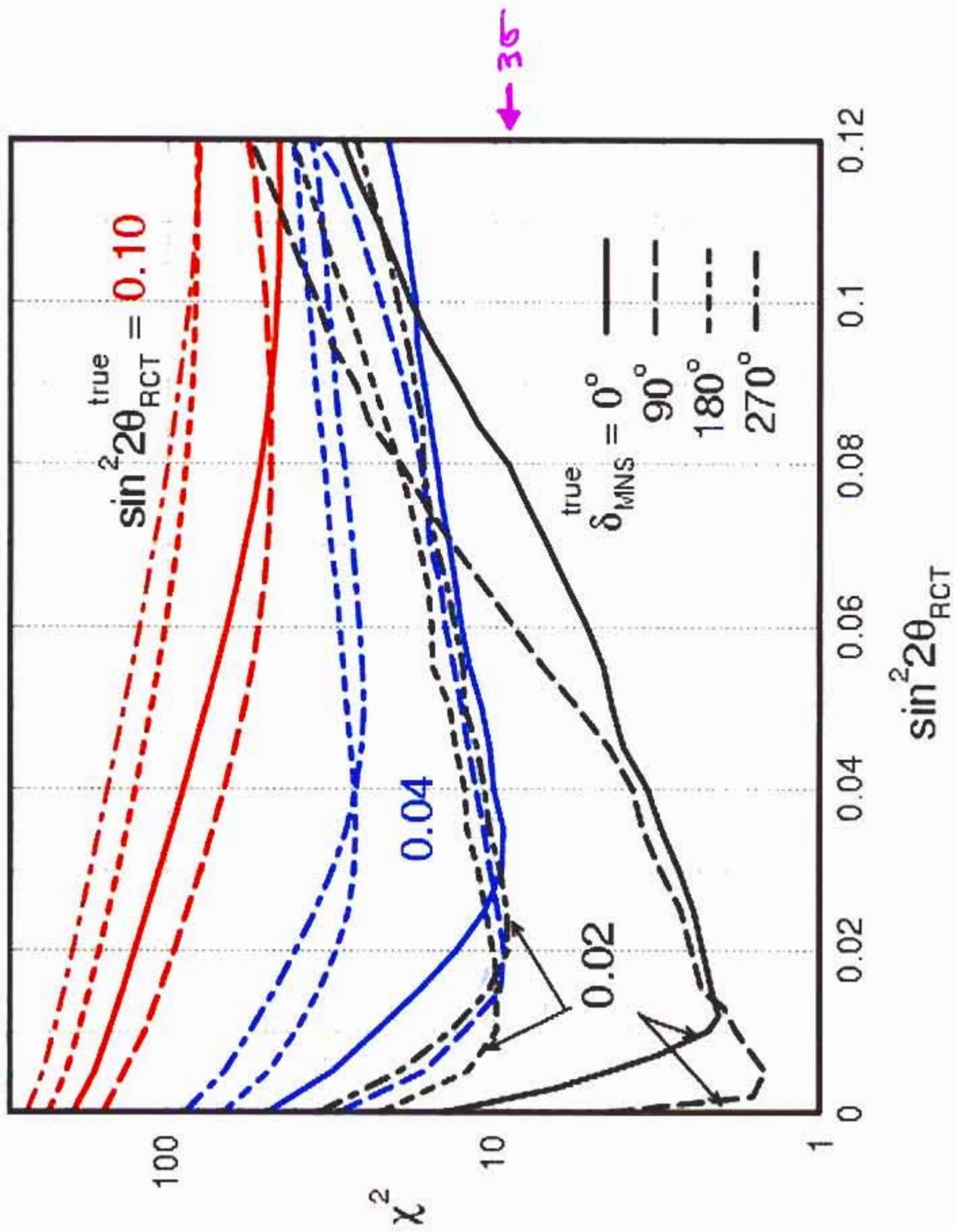
(b) NBB ( $E_{\text{peak}}=6\text{GeV}$ ) at  $L=2100 \text{ km}$



JPARC-to-Beijing

M. Akhmedov et al, PRD 67: 093004 (2003)

2100km & 295km Nor.(true) vs. Inv.(fit)

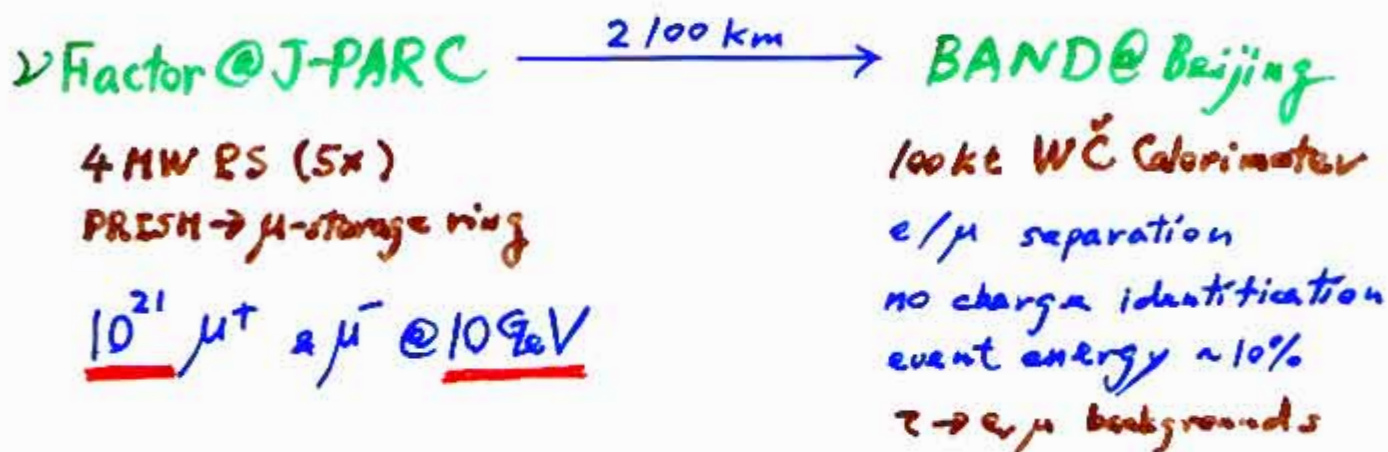




## Remaining problems:

- mass hierarchy : what if  $\sin^2 2\theta_{\text{RCT}} < 0.04$ ?
- $\delta_{\text{MNS}} = 0^\circ$  vs  $180^\circ$  : we may want 3 $\sigma$  resolution
- $\sin^2 \theta_{\text{ATM}} \gtrless \frac{1}{2}$  : how powerful will new reactor experiments? <sup>be</sup>

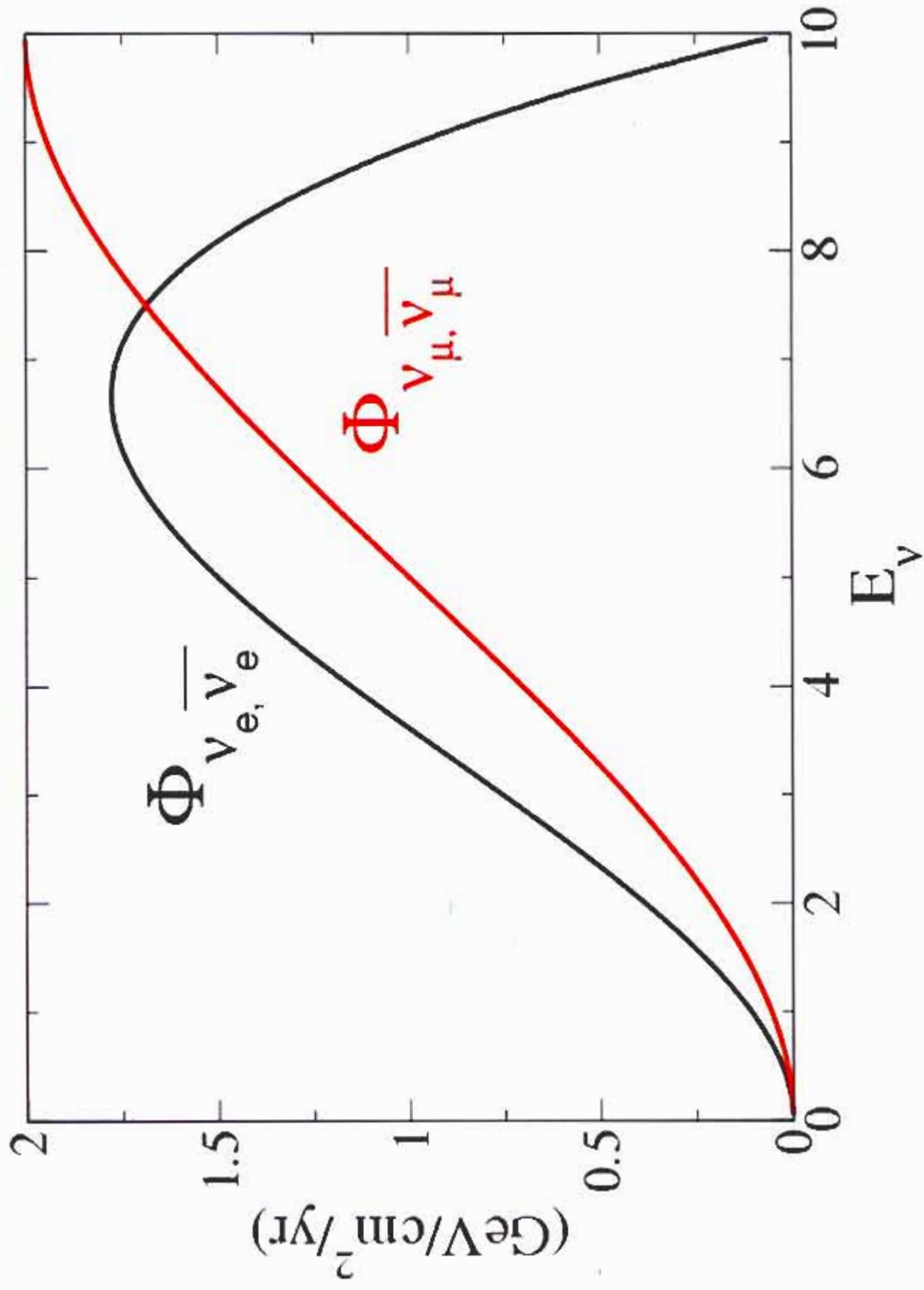
Our proposal : M. Aoki, K.H. N. Okamura, hep-ph/0311324



- $m_3 \gtrless m_1$  resolved if  $\sin^2 2\theta_{\text{RCT}} > 0.004$
- $\delta_{\text{MNS}} = 0^\circ \leftrightarrow 180^\circ$  resolved if  $\sin^2 2\theta_{\text{RCT}} > 0.02$
- $\sin^2 \theta_{\text{ATM}} \gtrless \frac{1}{2}$  resolved if  $\sin^2 2\theta_{\text{RCT}} > 0.02$   
for  $\sin^2 2\theta_{\text{ATM}} < 0.96$

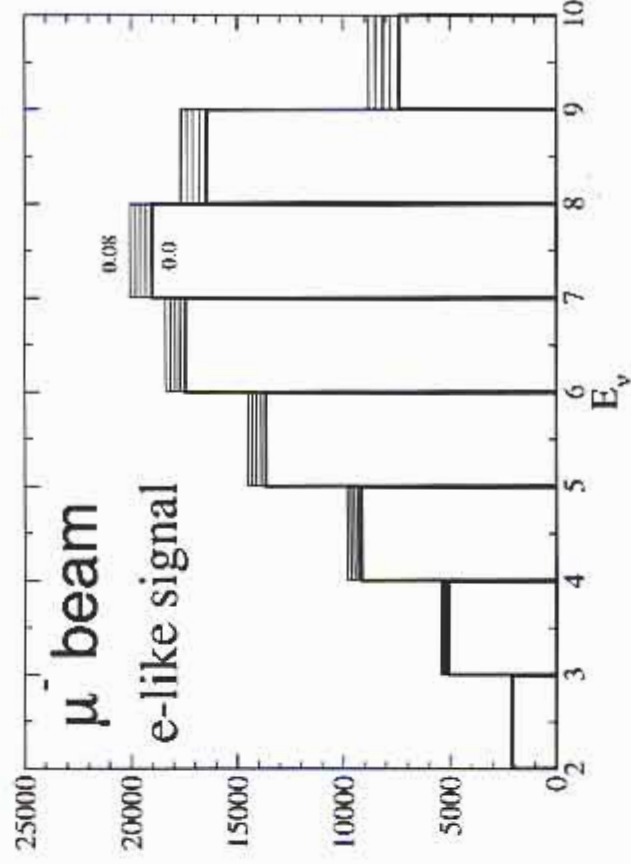
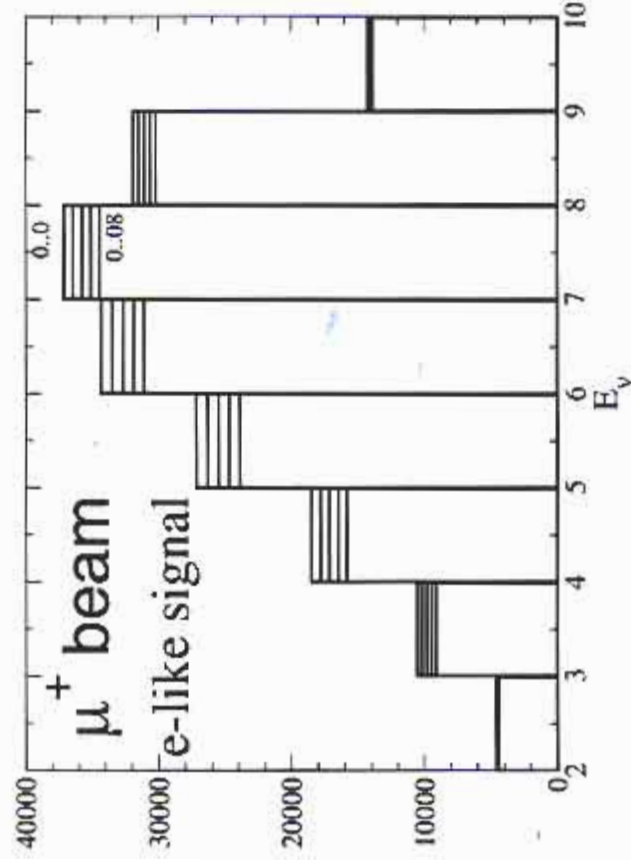
$L=2100$  km

$\mu^- \rightarrow e^- \nu_\mu \bar{\nu}_e$   
 $\mu^+ \rightarrow e^+ \bar{\nu}_\mu \nu_e$

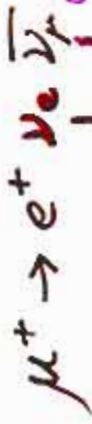


# $\nu$ Factory - to - Beijing

$$\sin^2 2\theta_{\text{RCT}} = 0, 0.02, 0.04, 0.06, 0.08$$



*suppressed by the matter effect*



*enhanced by the matter effect*



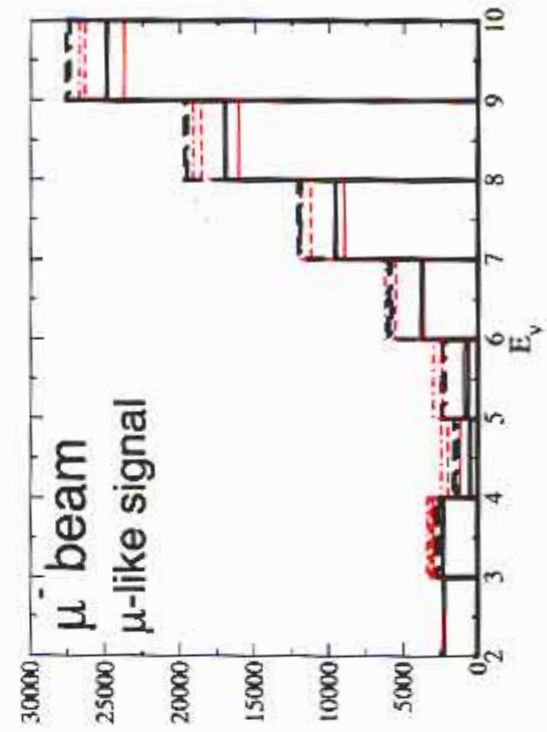
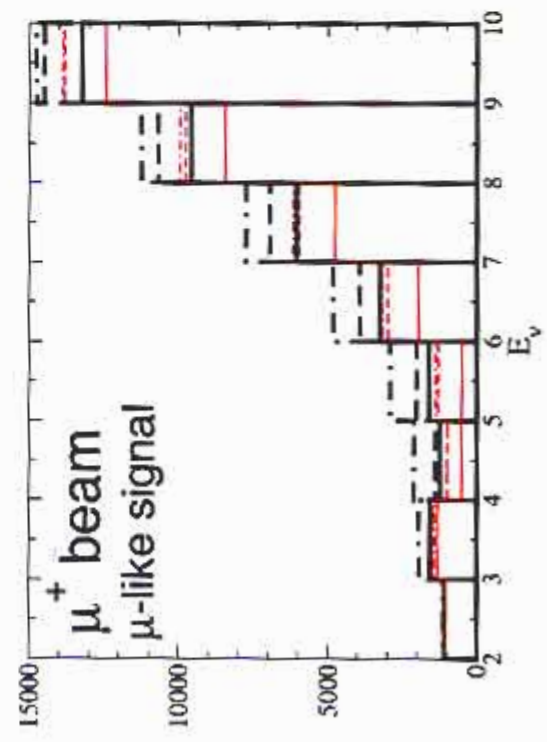
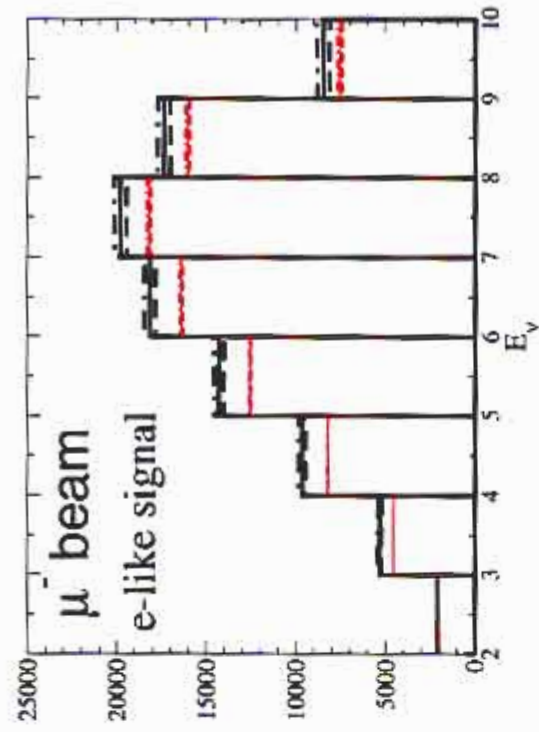
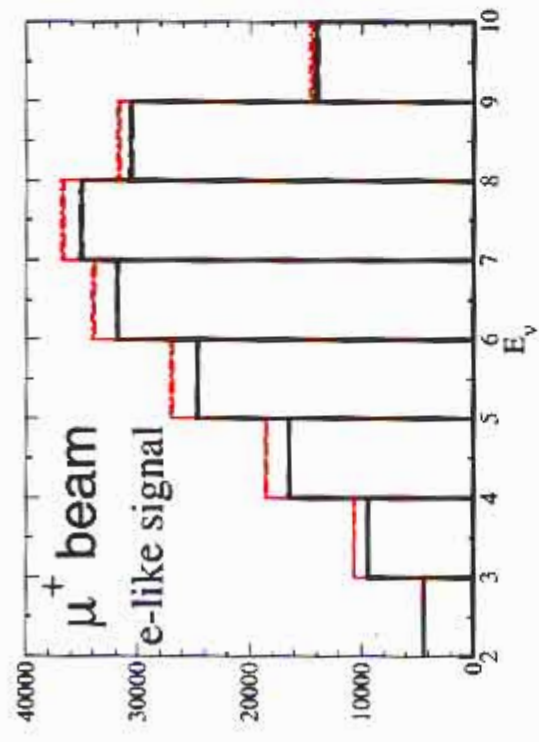
# Factory-to-Beijing

$m_1 < m_3$  normal  
 $m_1 > m_3$  inverted

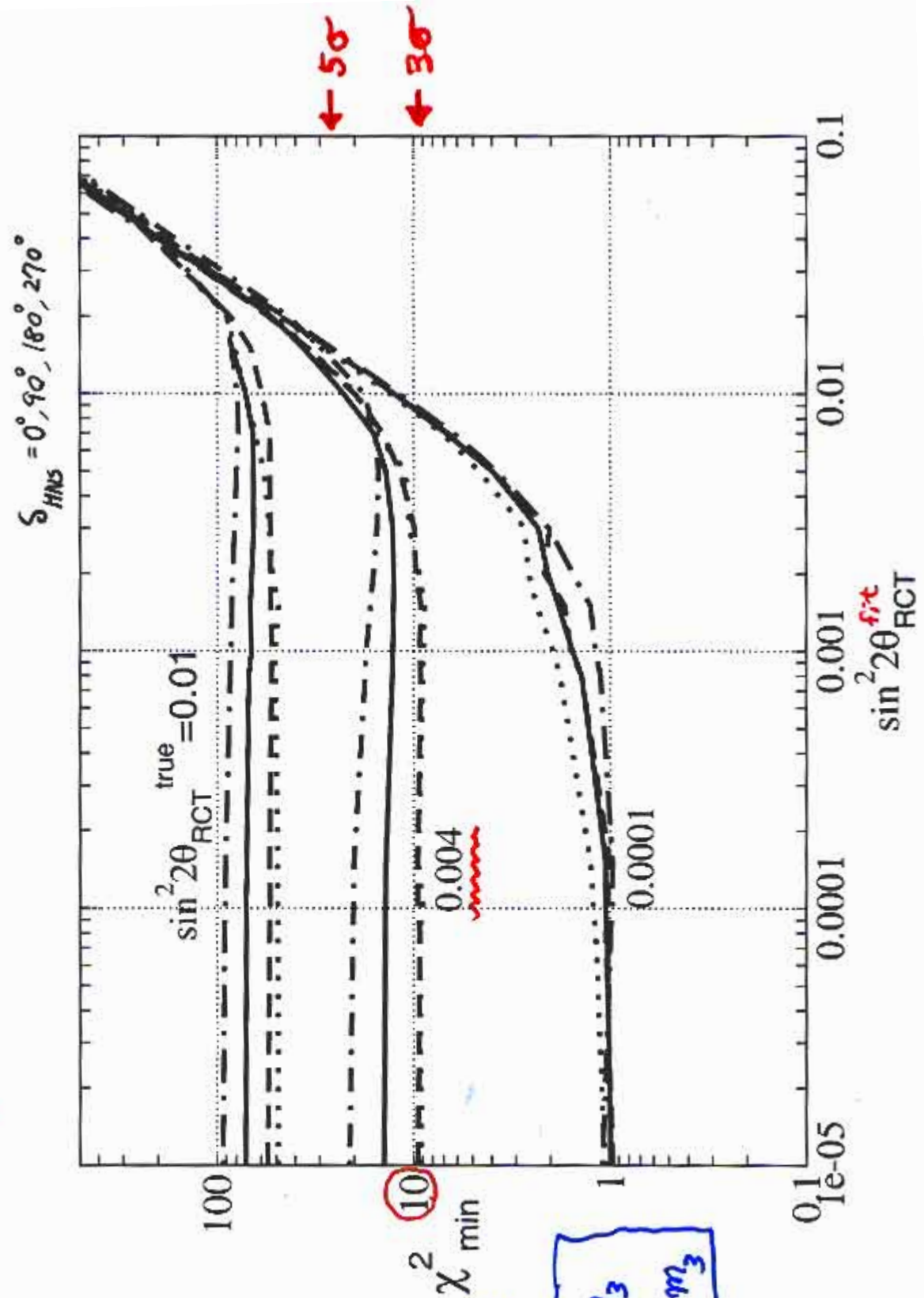
e-like signals are sensitive to  $m_1 \gtrsim m_3$

$\mu$ -like signals are sensitive to  $\sin^2 \theta_{ATM} \gtrsim \frac{1}{2}$

$\sin^2 \theta_{ATM}$   
 $= \begin{cases} 0.35 & \text{---} \\ 0.5 & \text{---} \\ 0.65 & \text{-.-.-} \end{cases}$

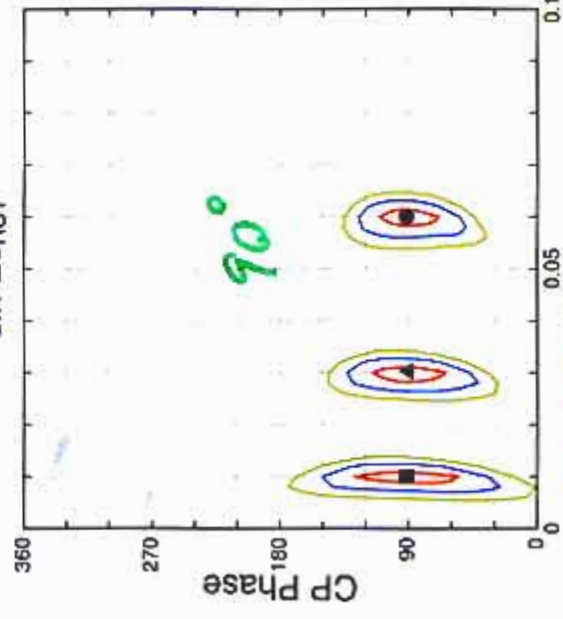
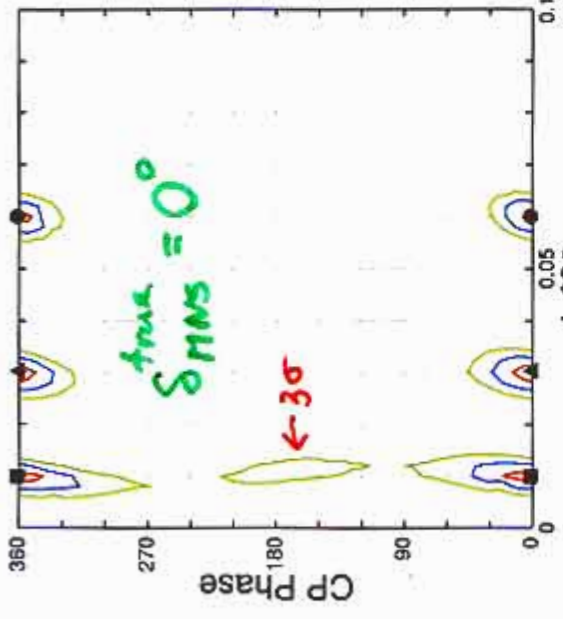
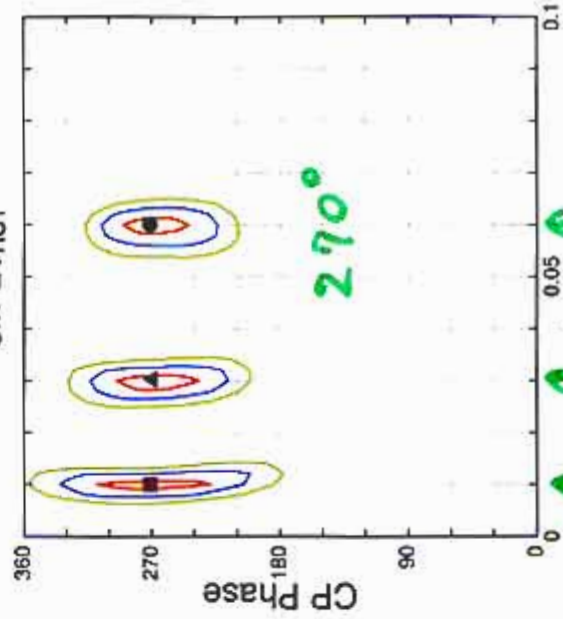
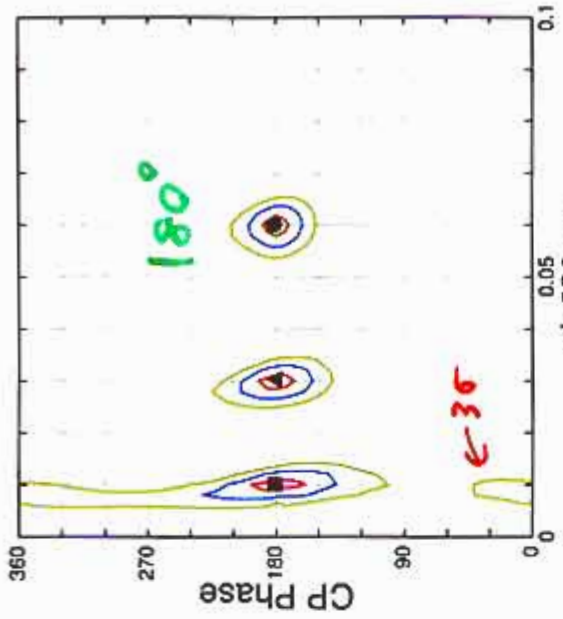


Factory-to-Beijing



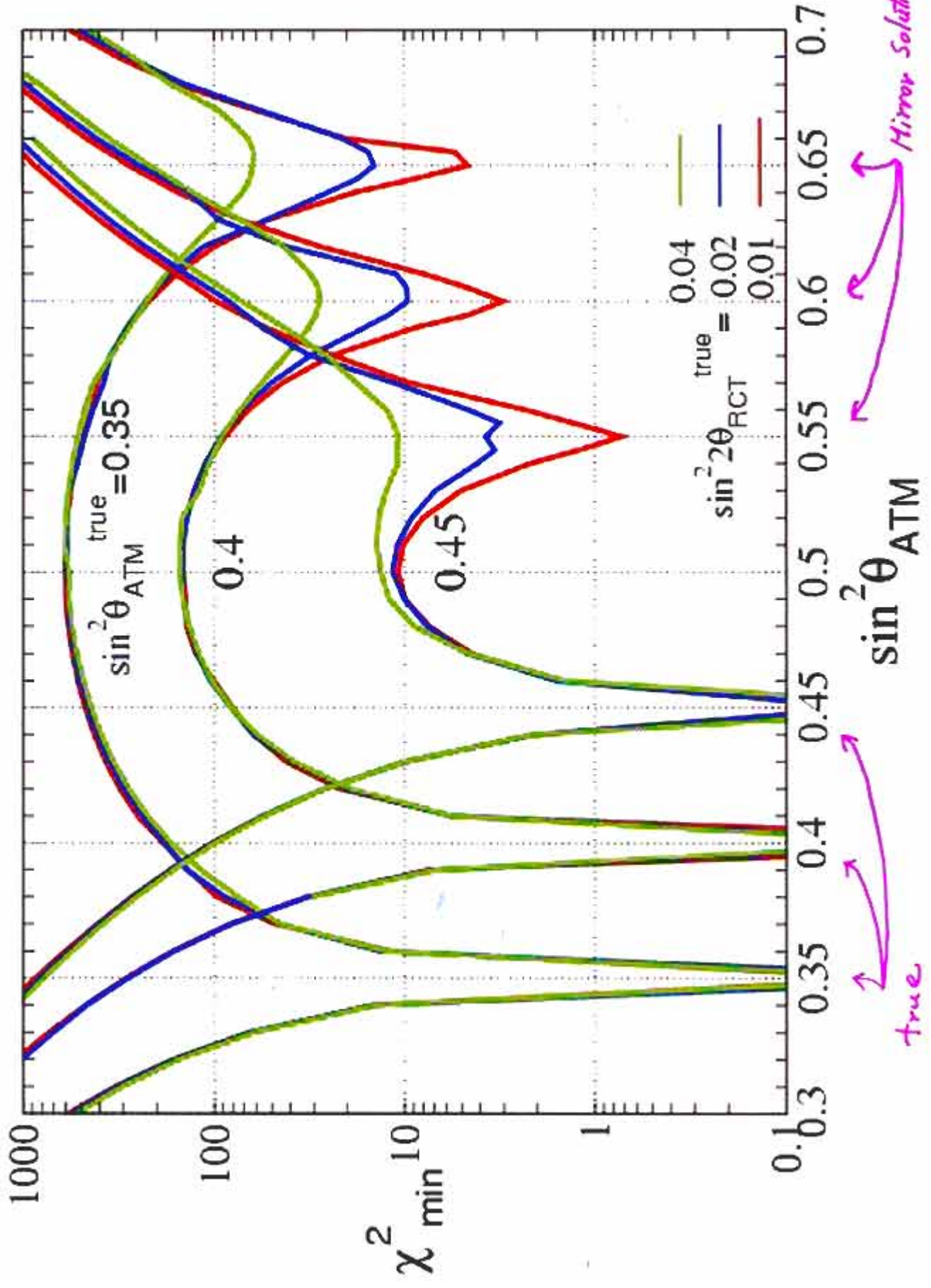
Data  $m_1 < m_3$   
 Analysis  $m_1 > m_3$

# Factory-to-Beijing



$\uparrow \uparrow \uparrow \sin^2 2\theta_{RCT}$   
 0.01 0.03 0.06  
 $\sin^2 2\theta_{RCT}$

*$\nu$  Factory-to-Beijing*



In the vacuum :

$$(1 - \sin^2 \theta_{RCT})^2 > \sin^2 2\theta_{SOL} \sim 0.8$$

$$P(\nu_e \rightarrow \nu_e) = 1 - 4 \underbrace{|U_{e3}|^2}_{\sin^2 \theta_{RCT}} (1 - |U_{e3}|^2) \sin^2 \left( \frac{\delta m_{13}^2}{4E} L \right) + \dots$$

$$\sin^2 \theta_{RCT} = \frac{1 - \sqrt{1 - \sin^2 2\theta_{RCT}}}{2}$$

$$P(\nu_\mu \rightarrow \nu_\mu) = 1 - 4 \underbrace{U_{\mu 3}^2}_{\sin^2 \theta_{ATM}} (1 - U_{\mu 3}^2) \sin^2 \left( \frac{\delta m_{13}^2}{4E} L \right) + \dots$$

$$\sin^2 \theta_{ATM} = \frac{1 \pm \sqrt{1 - \sin^2 2\theta_{ATM}}}{2}$$

$$P(\nu_\mu \rightarrow \nu_e) = -4 \underbrace{U_{\mu 3}^2}_{\sin^2 \theta_{ATM}} \underbrace{|U_{e3}|^2}_{\sin^2 \theta_{RCT}} \sin^2 \left( \frac{\delta m_{13}^2}{4E} L \right) + \dots$$

Observation of  $P(\nu_\mu \rightarrow \nu_e)$  tells  $\sin^2 \theta_{RCT} \neq 0$

but the two-fold ambiguity in  $\sin^2 \theta_{ATM}$  leads to

→ two-fold ambiguity in  $\sin^2 \theta_{RCT}$  leads to

→ two-fold ambiguity in  $\delta m_{13}^2$

Unique determination of  $\sin^2 \theta_{RCT}$  requires  $P(\nu_e \rightarrow \nu_e), P(\bar{\nu}_e \rightarrow \bar{\nu}_e)$ :

↓  
ν-Factory @ DAND

Reactor experiment @ Kashiwazaki

$$\frac{L}{E} \approx \frac{1 \text{ km}}{0.005 \text{ GeV}} \approx 200 \text{ (km/GeV)}$$

$$\frac{\delta m^2}{4E} L = \frac{\pi}{2}$$

(km/GeV)

$\frac{L}{E}$

$L = 1 \text{ km}$

$L = 300 \text{ km}$

$L = 730 \text{ km}$

$L = 2100 \text{ km}$

$$\delta m^2 = 3 \times 10^{-3} \text{ eV}^2$$

400

2.5 MeV

0.75 GeV

1.8 GeV

5 GeV

$$2.5 \times 10^{-3} \text{ eV}^2$$

500

2 MeV

0.6 GeV

1.5 GeV

4 GeV

$$2 \times 10^{-3} \text{ eV}^2$$

600

1.7 MeV

0.5 GeV

1.2 GeV

3.5 GeV



# Conclusions:

- Among the 9 parameters of the 3-neutrino model

( 3 masses 3 angles 3 phases )

only 6 parameters ( 2 mass<sup>2</sup> differences  $m_2^2 - m_1^2$   $m_3^2 - m_1^2$   
 3 angles  $\sin^2 \theta_{SOL}, \sin^2 \theta_{ATM}, \sin^2 \theta_{RCT}$   
 1 phase  $\delta_{MNS}$  )

can be measured by  $\nu$ -oscillation experiments.

$0\nu\beta\beta$  decay  $\rightarrow$  1 constraint  
 cosmology  $\rightarrow$  hot dark matter, leptogenesis  
 flavor physics  $\rightarrow$  quark-lepton relations, ...

- Among the 6 observables
  - 2 are known uniquely  $m_2^2 - m_1^2 = \Delta m_{SOL}^2, \sin^2 \theta_{SOL}$
  - 2 are known 2-fold upto  $m_3^2 - m_1^2 = \pm \Delta m_{ATM}^2, \sin^2 \theta_{ATM} = \frac{1 \pm \sqrt{1 - \sin^2 2\theta_{ATM}}}{2}$
  - 1 is constrained  $\sin^2 \theta_{RCT} \lesssim 0.05$
  - 1 is unknown  $\delta_{MNS} = 0 \sim 360^\circ$

- K2K 2000~2005 confirmation of  $P(\nu_\mu \rightarrow \nu_\mu) \neq 1$
- MINOS 2005~ precise measurement of  $\Delta m_{ATM}^2, \sin^2 2\theta_{ATM}$
- OPERA, ICARUS 2006~ confirmation of  $P(\nu_\mu \rightarrow \nu_e) \neq 0$

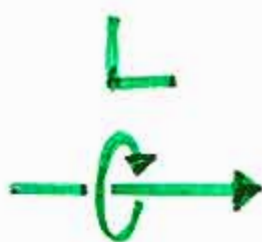
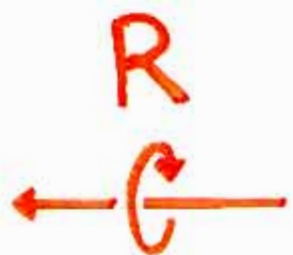
- J-PARC  $\rightarrow$  SK 2009~ precise measurement of  $\Delta m_{ATM}^2, \sin^2 2\theta_{ATM}$   
 detection of  $P(\nu_\mu \rightarrow \nu_e) \neq 0 \Rightarrow \sin^2 \theta_{RCT} \neq 0$  2-fold  
 Korea ?

- Reactor exp. @ Kashiwanaki  $P(\bar{\nu}_e \rightarrow \bar{\nu}_e) \neq 1 \Rightarrow \sin^2 \theta_{RCT} \neq 0$  uniquely

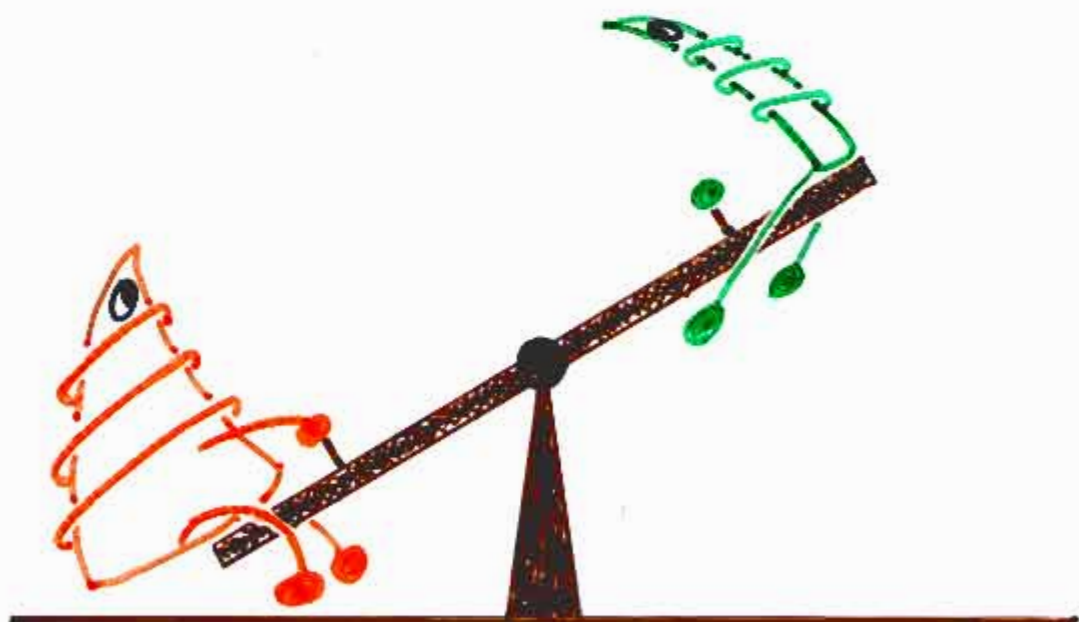
- J-PARC  $\rightarrow$  Hyper-Kamiokande  $P(\nu_\mu \rightarrow \nu_e) \neq P(\bar{\nu}_\mu \rightarrow \bar{\nu}_e) \Rightarrow \delta_{MNS}, \sin^2 \theta_{RCT}$   
 4-fold ambiguity

- J-PARC  $\rightarrow$  BAND @ Beijing  $P(\nu_\mu \rightarrow \nu_e) \neq 0 \Rightarrow m_3^2 - m_1^2 \geq 0$  if  $\sin^2 2\theta_{RCT} \geq 0.04$

- $\nu$  Factory @ J-PARC  $\rightarrow$  BAND  $P(\nu_e \rightarrow \nu_e) \neq 0$  etc  $\Rightarrow m_3^2 - m_1^2 \geq 0$  if  $\sin^2 2\theta_{RCT} \geq 0.004$   
 $\sin^2 \theta_{ATM} \geq \frac{1}{2}$  if  $\sin^2 2\theta_{RCT} \geq 0.02$   
 for  $\sin^2 2\theta_{ATM} = 0.96$ .



1979



2004. 2. 23-25 @ KEK

See Saw 25 years